# UNIVERSITY OF CALIFORNIA <br> College of Engineering <br> Department of Electrical Engineering and Computer Sciences 

Final Exam

May 17, 2000

## EECS 240

SPRING 2000

Show derivations and mark results with box around them. Erase or cross-out erroneous attempts. Mark your name and SID at the top of the exam sheet.

1. [ 30 points] All component values in the amplifiers below are identical except for $\mathrm{g}_{\mathrm{m} 2}$, which is adjusted for 63 degrees phase margin with unity-gain feedback. Calculate the ratio of $g_{m 2}$ for amplifier A to $g_{m 2}$ for amplifier $B$ as a function of $C_{G S 1}, C_{G S 2}, C_{1}, C_{2}$, $\mathrm{C}_{\mathrm{L}}$. Treat all non-given parameters as ideal.


Amplifier A


Amplifier B
2. [15 points] The circuit below is "perfectly" symmetrical except for capacitor $\mathrm{C}_{\mathrm{x}}$ that was inadvertently added due to a layout error. Calculate $\mathrm{V}_{\text {od }}$ for $\mathrm{V}_{\mathrm{id}}=0$ just before the end of phase $\Phi_{2}$. All transistors are NMOS, the amplifier is ideal, and $\Phi_{1}$ and $\Phi_{2}$ are 0 V to 3 V non-overlapping clocks.

3. [30 points] The amplifier below is placed in a negative unity-gain feedback loop (i.e. $\mathrm{v}_{\mathrm{i}}=-\mathrm{v}_{\mathrm{o}}$ ).
a) Calculate the total output noise delivered to $\mathrm{C}_{2}$ in V-rms as a function of $\mathrm{g}_{\mathrm{m} 1}, \mathrm{~g}_{\mathrm{m} 3}$, $\mathrm{C}_{1}, \mathrm{C}_{2}$. Ignore the noise from M3, flicker noise and all capacitors except $\mathrm{C}_{1}$ and $\mathrm{C}_{2}$. All devices operate in the forward-active region and $\mathrm{g}_{\mathrm{m}} \mathrm{r}_{\mathrm{o}} \gg 1$.
Note: M3 usually contributes more noise than M1 and M2 combined, but the math is a little too tedious to be appropriate for an exam: do only if you are done with all other problems.
b) Calculate the ratio $g_{m 1} / g_{m 3}$ required for a 63-degree phase margin with unity-gain feedback.

4. [25 points] All transistors in the circuit below operate in the forward active region, have nominally the same W/L, and are biased at $\mathrm{V}_{\mathrm{dsat}}=200 \mathrm{mV}$ (assume "square-law characteristics"). All devices are subject to the following random variations:
$\sigma_{\text {VTH } 0}=2 \mathrm{mV}, \sigma_{\Delta(\mathrm{W} / \mathrm{L}) /(\mathrm{W} / \mathrm{L})}=0.2 \%, \sigma_{\Delta R / \mathrm{R}}=0.5 \%, \sigma_{\gamma}=0.01 \mathrm{~V}^{1 / 2}$.
Device Parameters: $\Phi_{\mathrm{f}}=0.3 \mathrm{~V}, \lambda \rightarrow$ infinity.
a) Calculate the standard deviation of the input referred offset voltage, $\sigma_{V \text { os }}$ at low frequency for $\mathrm{V}_{\mathrm{X}}=0 \mathrm{~V}$ and $\mathrm{V}_{\mathrm{X}}=3 \mathrm{~V}$. Assume that the mismatch is small compared to the mean for all parameters.
b) Assuming $\sigma_{V o s}=5 \mathrm{mV}$ (not the correct answer for part a), what is the fraction of amplifiers with an offset voltage less than 2 mV ?


