

**UNIVERSITY OF CALIFORNIA**  
**College of Engineering**  
**Department of Electrical Engineering and Computer Sciences**

EECS 130  
Spring 2009

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## Midterm I

Name: \_\_\_\_\_

*Closed book. One sheet of notes is allowed.*  
*There are ten pages of this exam including this page.*

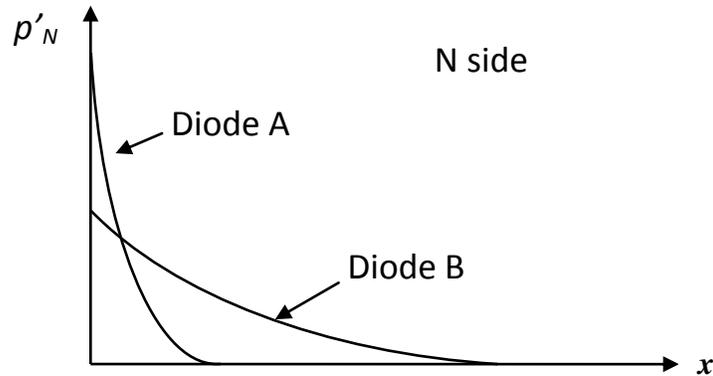
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<b>Problem 3</b>		35
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<b>Total</b>		100

## Physical Constants

Electronic charge	$q$	$1.602 \times 10^{-19} \text{ C}$
Permittivity of vacuum	$\epsilon_0$	$8.845 \times 10^{-14} \text{ F cm}^{-1}$
Relative permittivity of silicon	$\epsilon_{\text{Si}}/\epsilon_0$	11.8
Boltzmann's constant	$k$	$8.617 \times 10^{-5} \text{ eV/ K}$ or $1.38 \times 10^{-23} \text{ J K}^{-1}$
Thermal voltage at $T = 300\text{K}$	$kT/q$	0.026 V
Effective density of states	$N_c$	$2.8 \times 10^{19} \text{ cm}^{-3}$
Effective density of states	$N_v$	$1.04 \times 10^{19} \text{ cm}^{-3}$
Silicon Band Gap	$E_G$	1.1 eV
Intrinsic carrier concentration of Si at 300K	$n_i$	$10^{10} \text{ cm}^{-3}$

### Problem 1

Minority carrier concentration versus position plots are often used to describe the situation inside semiconductor devices. A linear plot of the excess minority carrier concentration on the N-side of two ideal P<sup>+</sup>-N diodes maintained at room temperature is pictured below. The P-side doping ( $N_a$ ), N-side doping ( $N_d$ ) and the cross-sectional area are the same in both diodes. Assume low-level injection conditions prevail.



- (a) Are both diodes forward, zero, or reverse biased? [3pts]

Forward bias

- (b) Which diode has higher bias? Briefly explain. [5pts]

Diode A.  $p'_N(0) = p_{N0} \left( e^{\frac{qV}{kT}} - 1 \right)$ , since  $p'_{NA}(0) > p'_{NB}(0)$  and  $p_{N0A} = p_{N0B} \rightarrow V_A > V_B$

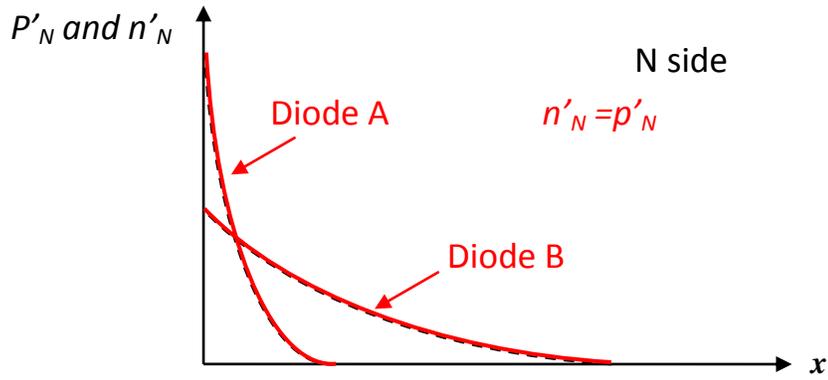
- (c) Which diode has higher minority carrier lifetime on the N-side? Assume that the hole mobility of diode A and B are the same. Briefly explain. [5pts]

Diode B.  $L = \sqrt{D\tau}$ , since  $L_B > L_A$  and  $D_A = D_B$  ( $\mu_A = \mu_B$ )  $\rightarrow \tau_B > \tau_A$

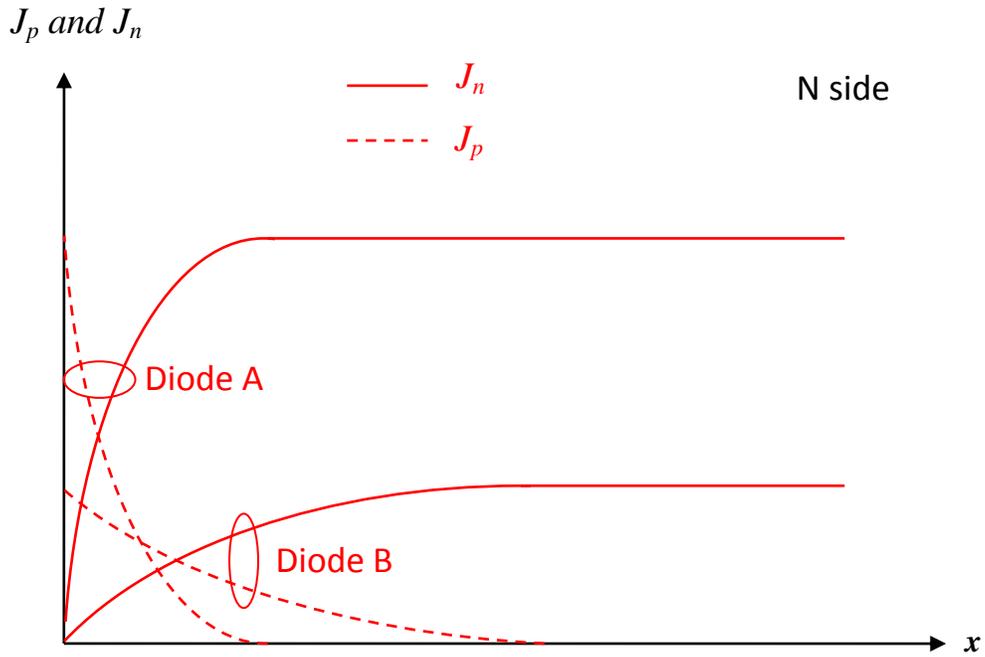
- (d) Which diode has higher current? Briefly explain. [5pts]

Diode A.  $J_p = -qD \frac{dp'}{dx}$ , since  $D_A = D_B$  and  $\left| \frac{dp'_A}{dx} \right| > \left| \frac{dp'_B}{dx} \right| \rightarrow J_{pA} > J_{pB}$

- (e) Given the plot of  $p'_N$  in dashed lines in the following figure, add  $n'_N$  in solid lines for diode A and B and label them. [4pts]



- (f) Qualitatively draw  $J_p$  and  $J_n$  for diode A and B. Label them clearly. [8pts]

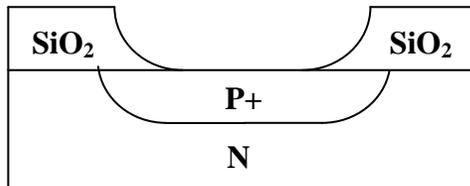


## Problem 2

- (a) Given below is a menu consisting of various fabrication processes you are familiar with. Using only these given processes, complete the sequence of steps to fabricate the structure given below. (Hint: All given processes may or may not be required, and the same process maybe used multiple times.)

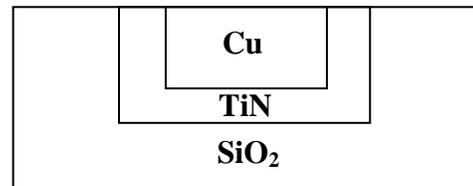
Processes Available:

Thermal annealing (diffusion)	Epitaxy	Anisotropic Etching
CVD (Chemical Vapor Deposition)	Isotropic Etching	Nanoimprint
CMP (Chemical-mechanical polishing)	Lithography	Thermal oxidation
ALD (Atomic layer deposition)	Ion implantation	Sputtering



Starting from a N-type silicon wafer [5pts]

Thermal oxidation  
Lithography  
Isotropic Etching  
Ion implantation  
Thermal annealing



Starting from SiO<sub>2</sub> [5pts]

Lithography  
Anisotropic Etching  
Sputter TiN  
CVD Cu  
CMP

- (b) Briefly explain the difference between positive and negative photoresists. [4pts]

The exposed regions are removed for positive photoresist, while the unexposed regions are removed for negative photoresist.

- (c) Why does wet lithography provide better resolution? Briefly explain. [3pts]

When light enters the water, its wavelength is reduced by the refraction index of water, 1.43, and therefore the lithography resolution is improved. (lithography resolution =  $k\lambda$ )

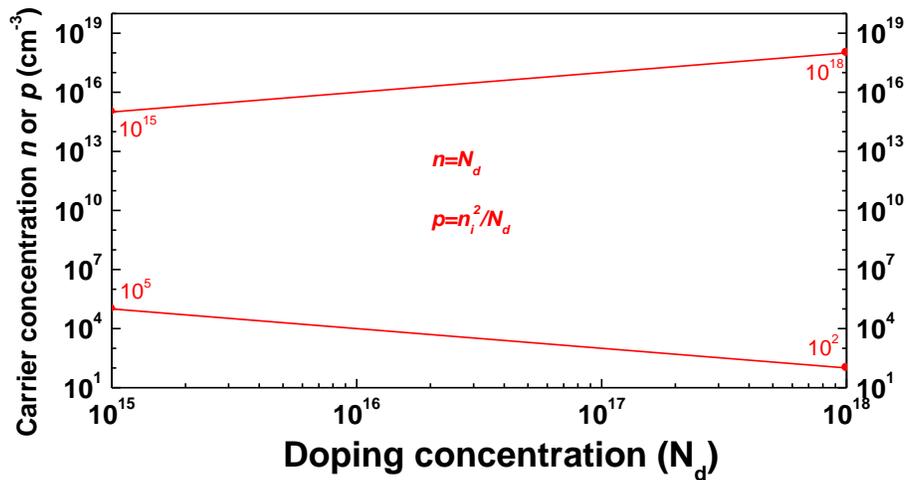
- (d) What motivates the IC industry to use increasingly larger silicon wafer size? Briefly explain. [3pts]

More dies of chip can be sliced out of a larger wafer size. Therefore the cost per chip is reduced.

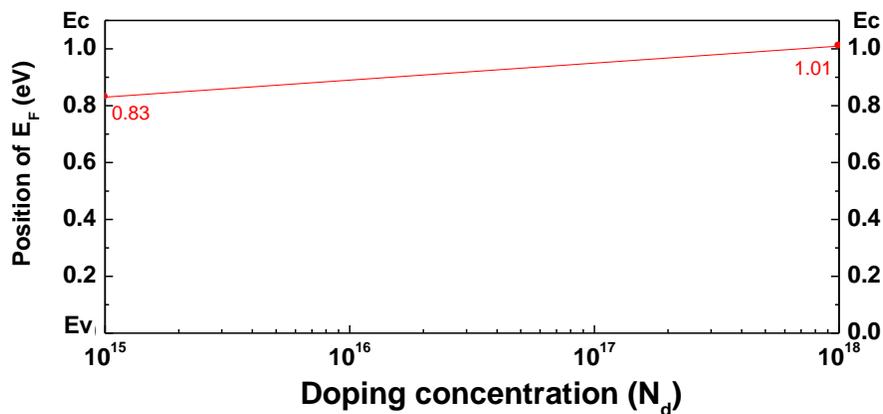
### Problem 3

Doping concentration plays an important role in changing the physical and electrical properties of a doped semiconductor. You are given an N-type silicon semiconductor:

- (a) Draw carrier concentrations  $n$  and  $p$  versus doping concentration in  $T=300\text{K}$ . Do the calculation to specify the left and right intercept of the line. [4pts]



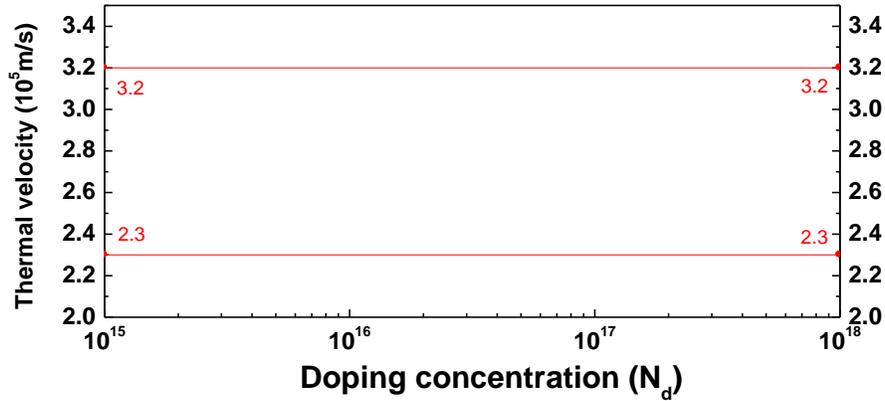
- (b) Draw the position of Fermi level versus doping concentration in  $T=300\text{K}$ . Do the calculation to specify the left and right intercept of the line. [7pts]



$$n = N_d = N_c \exp\left(\frac{E_F - E_c}{kT}\right)$$

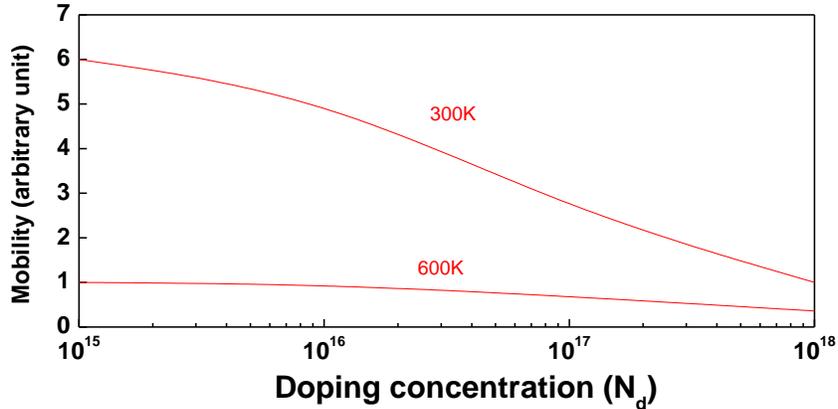
$$\Rightarrow E_F = E_c + kT \times \ln\left(\frac{N_d}{N_c}\right)$$

- (c) Thermal velocity at  $T=300\text{K}$  and  $N_d=10^{15}\text{ cm}^{-3}$  is  $2.3\times 10^5\text{ m/s}$ . Draw thermal velocity versus doping concentration in  $300\text{K}$  and  $580\text{K}$ . Do the calculation to specify the intercepts of the lines. [4pts]



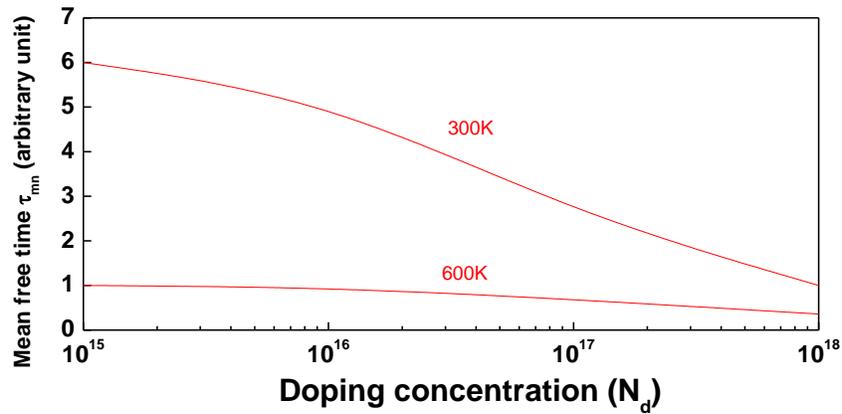
$$v_{th} = \sqrt{\frac{3kT}{m}} \propto \sqrt{T}, \text{ therefore it's independent of doping concentration}$$

- (d) i. Qualitatively draw electron mean free time versus doping concentration at  $300\text{K}$  and  $600\text{K}$ , given that  $\tau_{mn}$  at  $300\text{K}$ ,  $10^{15}\text{ cm}^{-3}$  is six times of  $\tau_{mn}$  at  $600\text{K}$ ,  $10^{15}\text{ cm}^{-3}$ . (No need to do calculations) [4pts]



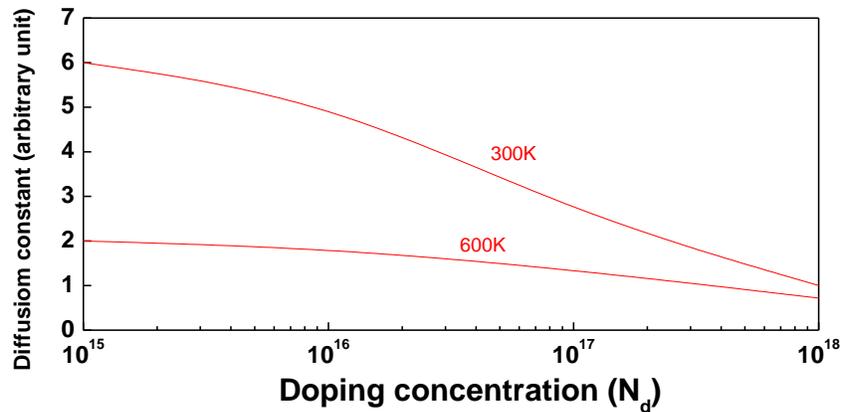
- ii. At  $300\text{K}$ , what scattering mechanism dominates at low ( $10^{15}\text{ cm}^{-3}$ ) and high ( $10^{18}\text{ cm}^{-3}$ ) doping concentration respectively? [3pts]
- Low ( $10^{15}\text{ cm}^{-3}$ ): Phonon scattering  
 High ( $10^{18}\text{ cm}^{-3}$ ): Columbic (impurity) scattering
- iii. At  $600\text{K}$ , what scattering mechanism dominates at low ( $10^{15}\text{ cm}^{-3}$ ) and high ( $10^{18}\text{ cm}^{-3}$ ) doping concentration respectively? [3pts]
- Low ( $10^{15}\text{ cm}^{-3}$ ): Phonon scattering  
 High ( $10^{18}\text{ cm}^{-3}$ ): Phonon and impurity both have effect (free 1.5 points !)

- (e) Qualitatively draw electron mobility versus doping concentration at 300K and 600K. Briefly explain how you get the curves. (No need to do calculations) [4pts]



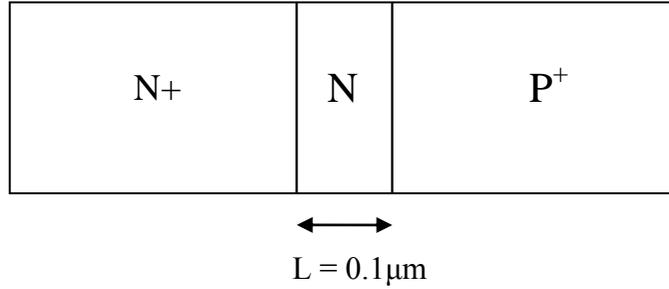
$\mu_n = \frac{q\tau_{mn}}{m_n}$ , therefore mobility curves are the same shape of mean free time.

- (f) Qualitatively draw electron diffusion constant versus doping concentration at 300K and 600K. Briefly explain how you get the curves. [6pts]



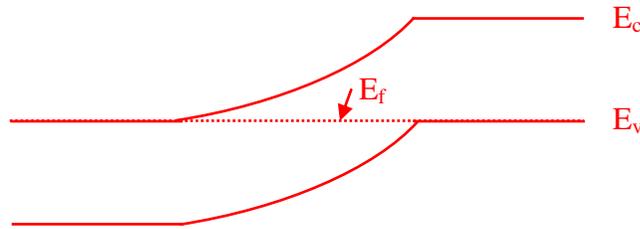
$D_n = \frac{kT}{q} \mu_n$ , therefore, the diffusion constant curves are the same shape except the one at 600K should be doubled up the value.

**Problem 4**



Consider the above silicon diode. Assume that  $N^+$  and  $P^+$  regions are heavily doped that  $E_c = E_f$  in the  $N^+$  region and  $E_F = E_v$  in the  $P^+$  region. The doping in the N-type region is  $5 \times 10^{16} \text{ cm}^{-3}$ . Assume that the N layer is thin enough that it is completely depleted.

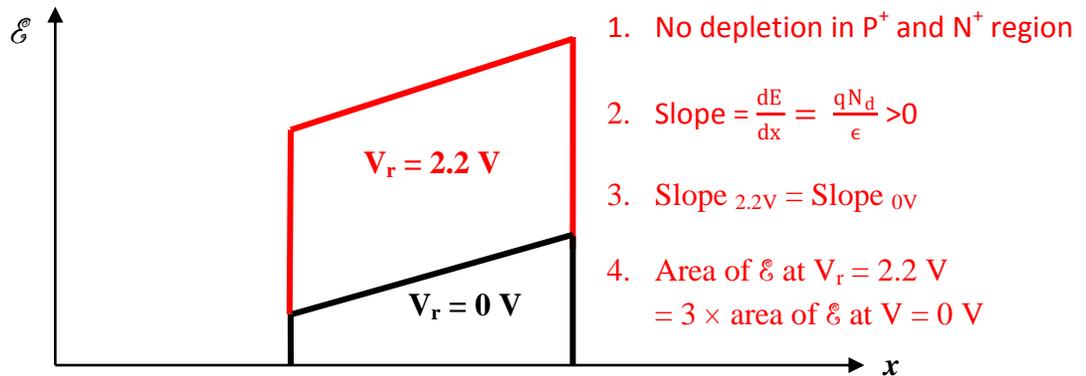
- (a) Sketch the energy band diagram for this diode. Do not be concerned with the exact shape of  $E_c(x)$  in the depletion region. [2pts]



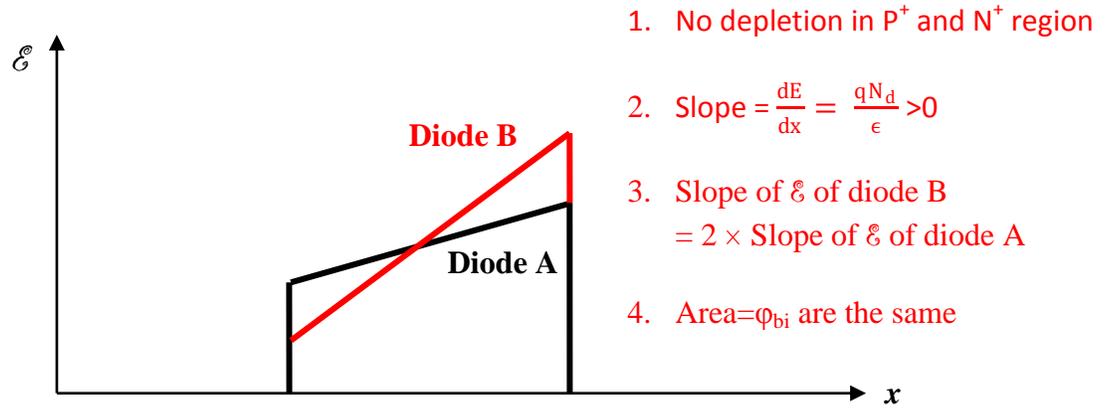
- (b) Find the built in potential ( $\phi_{bi}$ ) of the given diode in Volts. [2pts]

**Built in potential ( $\phi_{bi}$ ) = Bandgap =  $E_g/q = 1.1 \text{ V}$**

- (c) Qualitatively draw the electric field in the semiconductor as a function of  $x$  under the condition of (i)  $V=0\text{V}$  (ii)  $V_r$  (reverse bias) =  $2.2 \text{ V}$  on the same plot. (Hint: You may assume that the depletion region is entirely contained in the N region only. No need to do calculation) [4pts]



(d) Call the diode in part (a) “diode A”. Now consider another “diode B” with the identical  $N^+-N-P^+$  structure except doping of N region is  $10^{17} \text{ cm}^{-3}$ . Qualitatively draw the electric field at  $V=0V$  of diodes A and B as a function of  $x$  in the same plot. [4pts]



(e) Does diode A or B has higher breakdown voltage? Briefly explain why. [3pts]

Diode A has a higher breakdown voltage.  
Because diode A has a lower peak electric field at a given bias.  
Therefore, diode A has to reach  $E_{crit}$  ( $E_{critA} = E_{critB}$ ) at a higher voltage.