## Problem 1

Your construction company needs to purchase a new steamroller. You consider three major steamroller manufacturers. Considering a MARR of $12 \%$, which manufacturer should you purchase from if you plan to use this roller for 8 years? Explain your reasoning.

|  | A | B | C |
| :--- | :---: | :---: | :---: |
| Initial Cost | $\$ 125,034$ | $\$ 101,858$ | $\$ 119,565$ |
| Annual Revenue | $\$ 90,000$ | $\$ 30,000$ | $\$ 40,000$ |
| Annual Maintenance | $\$ 10,000$ | $\$ 15,000$ | $\$ 20,000$ |
| Salvage Value at $8 \mathbf{y r}$ | $\$ 60,000$ | $\$ 40,000$ | $\$ 50,000$ |

## Problem 2

An investment alternative is represented by the following cash flow:

| Time $=$ | Cash Flow |
| :---: | :---: |
| 0 | $-\$ 500$ |
| 1 | $\$ 0$ |
| 2 | $+\$ 1,649$ |
| 3 | $-\$ 700$ |
| 4 | $-\$ 500$ |

Analyze the IRR of this cash-flow and provide a recommendation if the MARR is:
(a) $12 \%$
(b) $15 \%$
(c) $20 \%$

## Problem 3

(a) With the help of a graph, explain how the level of influence and the cumulative cost of a project vary over the project life-cycle.
(b) Explain the difference between Design-Build and Design-Bid-Build project delivery methods using the level of influence concept.

## Problem 4

You deposit money once into a savings account at time $=0$ that has a nominal interest rate of $12 \%$.
(a) What is the effective interest rate of this savings account if compounded annually for 6 years?
(b) If this account is worth $\$ 858$ at the end of 5 years and the $12 \%$ nominal interest rate is compounded quarterly, how much money was initially deposited?

## Problem 5

(a) What does BIM stand for?
(b) What are three major advantages of BIM to a contractor?
(c) What are three major advantages of BIM to an owner?

## Problem 6

Explain the key differences between the Construction Management at risk and the professional Construction Management method of project delivery. Also draw their typical project organisation trees.

Name:

## Problem 7

Consider the following property investments under a discount rate of $12 \%$ :

|  | A | B |
| :--- | :---: | :---: |
| Initial Cost (in \$) | 60,000 | 70,000 |
| Life | $4 y r s$ | $8 y r s$ |
| Salvage Value (in \$) | 47,000 | 20,000 |
| Annual Revenue (in \$) | 20,000 | 18,000 |
| Annual Cost (in \$) | 10,000 | 8,000 |
| Discount Rate | $12 \%$ | $12 \%$ |

Which property would you recommend on the basis of the discounted payback method? Which one would you recommend on the basis of NPV?

## Reference Equations

- $[\mathbf{F} / \mathbf{P}, \mathbf{i}, \mathbf{n}]=(1+i)^{n}$
- $[\mathbf{F} / \mathbf{A}, \mathbf{i}, \mathbf{n}]=\frac{(1+i)^{n}-1}{i}$
- $[\mathbf{P} / \mathbf{A}, \mathbf{i}, \mathbf{n}]=\frac{(1+i)^{n}-1}{i(1+i)^{n}}$
- $[\mathbf{A} / \mathbf{P}, \mathbf{i}, \mathbf{n}]=\frac{i(1+i)^{n}}{(1+i)^{n}-1}$
- $i_{\text {eff }}=\left(1+\frac{i_{\text {nominal }}}{p}\right)^{p}-1$, where $\mathrm{p}=$ number of compounding periods per year

| $n$ | Single Payment |  | Uniform Payment Series |  |  |  | Arithmetic Gradient |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Compound Amount Factor Find $F$ Given $P$ F/P | Present <br> Worth <br> Factor Find $P$ <br> Given $F$ P/F | Sinking Fund Factor Find $A$ Given $F$ A/F | Capital Recovery Factor Find $A$ Given $P$ A/P | Compound Amount Factor Find $F$ Given $A$ F/A | Present <br> Worth <br> Factor Find $P$ <br> Given $A$ P/A | Gradient Uniform Series Find $A$ Given $\boldsymbol{G}$ A/G | Gradient <br> Present Worth Find $P$ Given $\boldsymbol{G}$ P/G | $n$ |
| 1 | 1.120 | . 8929 | 1.0000 | 1.1200 | 1.000 | 0.893 | 0 | 0 | 1 |
| 2 | 1.254 | . 7972 | . 4717 | . 5917 | 2.120 | 1.690 | 0.472 | 0.797 | 2 |
| 3 | 1.405 | . 7118 | . 2963 | . 4163 | 3.374 | 2.402 | 0.925 | 2.221 | 3 |
| 4 | 1.574 | . 6355 | . 2092 | . 3292 | 4.779 | 3.037 | 1.359 | 4.127 | 4 |
| 5 | 1.762 | . 5674 | . 1574 | . 2774 | 6.353 | 3.605 | 1.775 | 6.397 | 5 |
| 6 | 1.974 | . 5066 | . 1232 | . 2432 | 8.115 | 4.111 | 2.172 | 8.930 | 6 |
| 7 | 2.211 | . 4523 | . 0991 | . 2191 | 10.089 | 4.564 | 2.551 | 11.644 | 7 |
| 8 | 2.476 | . 4039 | . 0813 | . 2013 | 12.300 | 4.968 | 2.913 | 14.471 | 8 |
| 9 | 2.773 | . 3606 | . 0677 | . 1877 | 14.776 | 5.328 | 3.257 | 17.356 | 9 |
| 10 | 3.106 | . 3220 | . 0570 | . 1770 | 17.549 | 5.650 | 3.585 | 20.254 | 10 |


| 15\% | Compound Interest Factors |  |  |  |  |  |  |  | 15\% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Single Payment |  | Uniform Payment Series |  |  |  | Arithmetic Gradient |  |  |
| $n$ | Compound Amount Factor Find $F$ Given $P$ F/P | Present <br> Worth <br> Factor Find $P$ <br> Given $F$ P/F | Sinking Fund Factor Find $A$ Given $F$ A/F | Capital Recovery Factor Find $A$ Given $P$ A/P | Compound Amount Factor Find $F$ Given $A$ F/A | Present <br> Worth <br> Factor Find $P$ <br> Given $A$ $P / A$ | Gradient Uniform Series Find $A$ Given $\boldsymbol{G}$ A/G | Gradient <br> Present Worth Find $P$ Given $\boldsymbol{G}$ P/G | $n$ |
| 1 | 1.150 | . 8696 | 1.0000 | 1.1500 | 1.000 | 0.870 | 0 | 0 | 1 |
| 2 | 1.322 | . 7561 | . 4651 | . 6151 | 2.150 | 1.626 | 0.465 | 0.756 | 2 |
| 3 | 1.521 | . 6575 | . 2880 | . 4380 | 3.472 | 2.283 | 0.907 | 2.071 | 3 |
| 4 | 1.749 | . 5718 | . 2003 | . 3503 | 4.993 | 2.855 | 1.326 | 3.786 | 4 |
| 5 | 2.011 | . 4972 | . 1483 | . 2983 | 6.742 | 3.352 | 1.723 | 5.775 | 5 |
| 6 | 2.313 | . 4323 | . 1142 | . 2642 | 8.754 | 3.784 | 2.097 | 7.937 | 6 |
| 7 | 2.660 | . 3759 | . 0904 | . 2404 | 11.067 | 4.160 | 2.450 | 10.192 | 7 |
| 8 | 3.059 | . 3269 | . 0729 | . 2229 | 13.727 | 4.487 | 2.781 | 12.481 | 8 |
| 9 | 3.518 | . 2843 | . 0596 | . 2096 | 16.786 | 4.772 | 3.092 | 14.755 | 9 |
| 10 | 4.046 | . 2472 | . 0493 | . 1993 | 20.304 | 5.019 | 3.383 | 16.979 | 10 |
| 20\% |  |  |  | Compoun | Interest Facto |  |  |  | 20\% |


|  | Single Payment |  | Uniform Payment Series |  |  |  | Arithmetic Gradient |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $n$ | Compound Amount Factor Find $F$ Given $P$ F/P | Present <br> Worth <br> Factor <br> Find $P$ <br> Given $F$ P/F | Sinking Fund Factor Find $A$ Given $F$ A/F | Capital Recovery Factor Find $A$ Given $P$ A/P | Compound Amount Factor Find $F$ Given $A$ F/A | Present <br> Worth <br> Factor Find $P$ <br> Given $A$ P/A | Gradient Uniform Series Find $A$ Given $\boldsymbol{G}$ A/G | Gradient Present Worth Find $P$ Given $\boldsymbol{G}$ P/G | $n$ |
| 1 | 1.200 | . 8333 | 1.0000 | 1.2000 | 1.000 | 0.833 | 0 | 0 | 1 |
| 2 | 1.440 | . 6944 | . 4545 | . 6545 | 2.200 | 1.528 | 0.455 | 0.694 | 2 |
| 3 | 1.728 | . 5787 | . 2747 | . 4747 | 3.640 | 2.106 | 0.879 | 1.852 | 3 |
| 4 | 2.074 | . 4823 | . 1863 | . 3863 | 5.368 | 2.589 | 1.274 | 3.299 | 4 |
| 5 | 2.488 | . 4019 | . 1344 | . 3344 | 7.442 | 2.991 | 1.641 | 4.906 | 5 |
| 6 | 2.986 | . 3349 | . 1007 | . 3007 | 9.930 | 3.326 | 1.979 | 6.581 | 6 |
| 7 | 3.583 | . 2791 | . 0774 | . 2774 | 12.916 | 3.605 | 2.290 | 8.255 | 7 |
| 8 | 4.300 | . 2326 | . 0606 | . 2606 | 16.499 | 3.837 | 2.576 | 9.883 | 8 |
| 9 | 5.160 | . 1938 | . 0481 | . 2481 | 20.799 | 4.031 | 2.836 | 11.434 | 9 |
| 10 | 6.192 | . 1615 | . 0385 | . 2385 | 25.959 | 4.192 | 3.074 | 12.887 | 10 |

Mid Term 1 Solutions Steamraller $A$


$$
\begin{aligned}
N P V_{A} & =-125,034+(90,000-10,000)[P / A, 12 \%, 8]+(60,000)[P / F, 12 \%, 8] \\
& =-125,034+(80,000 \times 4.968)+(60,000 \times 0.4039) \\
& =-125,034+397,440+24,234 \\
& =+\$ 296,640
\end{aligned}
$$

Steamraller B

$\rightarrow$ Only

$$
\begin{aligned}
N P V_{B} & =-101,858+(30,000-15,000)[P / A, 12 \%, 8]+(40,000)[P / F, 12 \%, 8] \\
& =-101,858+(15,000 \times 4,968)+(40,000 \times 0.4039) \\
& =-101,858+74,520+16,156 \\
& =-\$ 11,182
\end{aligned}
$$

Steamraller C


$$
\begin{aligned}
N P V= & -500 \\
& +1649[P / F, i, 2] \\
& -700[P / F, i, 3] \\
& -500[P / F, i, 4]
\end{aligned}
$$

$$
\Rightarrow N P V=\frac{-500}{(1+i)^{\circ}}+\frac{1649}{(1+i)^{2}}-\frac{700}{(1+i)^{3}}-\frac{500}{(1+i)^{4}}
$$

@ $i=12 \%, N P V=-500.00$

$$
\begin{aligned}
& +1314.57 \\
& -498.25 \\
& -317.76 \\
& \hline-1.44
\end{aligned}
$$

@ $i=15 \%, N P V=-500.00$

$$
\begin{aligned}
& +1246.88 \\
& -460.26 \\
& -285.88 \\
& \hline+0.74
\end{aligned}
$$

$$
\begin{aligned}
@ i=20 \%, N P V & =-500.00 \\
& +1145.14 \\
& -405.09 \\
& -241.13 \\
& -1.08
\end{aligned}
$$

From figure 2, we get

$$
I R R_{1} \approx 14 \% \& I R R_{2} \approx 17 \%
$$

(a) If $M A R R=12 \%$,

$$
I R R_{1}, I R R_{2}>M A R R
$$

$\therefore$ Investment is favorable
(b) If $M A R R=15 \%$,


## Figure 1



Figure 2
$I R R_{1}<M A R R<I R R_{2}$
$\therefore$ Cannot make a recommendation
(c) If $M A R R=20 \%$,

$$
I R R_{1}, I R R_{2}<M A R R
$$

$\therefore$ Investment is not favorable

(a)

$$
\begin{aligned}
i_{e f f} & =\left(1+\frac{0.12}{1}\right)^{1}-1 \\
& =0.12 \text { OR } 12 \%
\end{aligned}
$$

(b)

$$
\begin{aligned}
& i=\frac{12 \%}{4}=3 \% \quad n=5 \text { years } \times 4 \text { quarters/year } \\
& =20 \\
& P=F\left[P / F, i_{i}^{35, n}\right] \\
& =\frac{858}{(1+0.03)^{20}} \\
& P=\$ 475.03
\end{aligned}
$$


$\frac{n-7}{22623}=\frac{8-n}{398} \rightarrow$ Choose option $A$; Option B does not break even $\therefore n=7.98$ years

$$
\begin{aligned}
N P V_{A}= & -60,000 \\
& +(20,000-10,000)[P / A, 12 \%, 8] \\
& -60,000[P / F, 12 \%, 4] \\
& +47,000[P / F, 12 \%, 4] \\
& +47,000[P / f, 12 \%, 8] \\
= & -60,000 \\
& +10,000(4.968) \\
& -60,000(0.6355) \\
& +47,000(0.6355) \\
& +47,000(0.4039) \\
= & +401.8
\end{aligned}
$$

$$
\begin{aligned}
N P V_{B}= & -70,000 \\
& +(18,000-8,000)[P / A, 12 \%, 8] \\
& +20,000[P / F, 12 \%, 8] \\
= & -70,000 \\
& +10,000(4,968) \\
& +20,000(0.4039) \\
= & -12,242
\end{aligned}
$$

$$
\begin{aligned}
& N P V_{A}>N P V_{B} \\
\rightarrow & \text { choose option } A
\end{aligned}
$$

