#### **UC Berkeley - Computer Science**

CS61BL: Data Structures Final, Summer 2017

This test has 11 questions worth a total of 60 points, and is to be completed in 170 minutes. The exam is closed book, except that you are allowed to use three double-sided page of notes as a cheat sheet (front and back). No calculators or other electronic devices are permitted. Give your answers and show your work in the space provided.

Write the statement out below in the blank provided and sign. You may do this before the exam begins. Any plagiarism, no matter how minor, will result in points deducted from your exam.

"I have neither given nor received any assistance during the taking of this exam."

I have neither given nor received any assistance during the taking of this exam.

Signature: LaVar Ball

Write your name and student ID on the front page. Write the names of your neighbors. Write and sign the above statement. Once the exam has started, write your class ID in the corner of every page.

Name: LaVar Ball Your Class ID: 495

SID: 9001 Name of person to left: Lonzo Ball

TA: LaVar Ball Name of person to right: LaMelo Ball

#### Tips:

- There may be partial credit for incomplete answers. Write as much of the solution as you can, but bear in mind that we may deduct points if your answers are much more complicated than necessary.
- There are a lot of problems on this exam. Work through the ones with which you are comfortable first. Do not get overly captivated by interesting design issues or complex corner cases you're not sure about.
- Not all information provided in a problem may be useful.
- Unless otherwise stated, all given code on this exam should compile. All code has been compiled and executed before printing, but in the unlikely event that we do happen to catch any bugs during the exam, we'll announce a fix. Unless we specifically give you the option, the correct answer is not 'does not compile.'
- indicates that only one circle should be filled in.
- Indicates that more than one box may be filled in.
- For answers that involve filling in a  $\bigcirc$  or  $\square$ , please fill in the shape completely.

Optional. Mark along the line to show your feeling	gs Before exam: [⊗	©].
on the spectrum between ⊕ and ⊕.	After exam: [⊖	©].

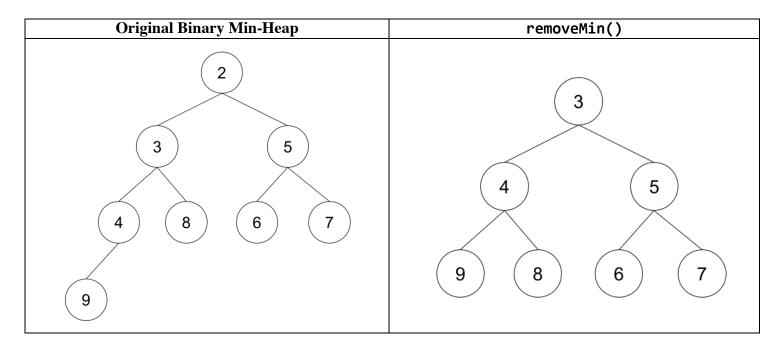
# 1. Steven the Pusheen (4 pts)

**a.** List the keys that are in the **ternary search trie** below in the middle box. Then, draw the result of inserting "HOT" into the ternary search trie. Mark the node that terminates the new key with a "T".

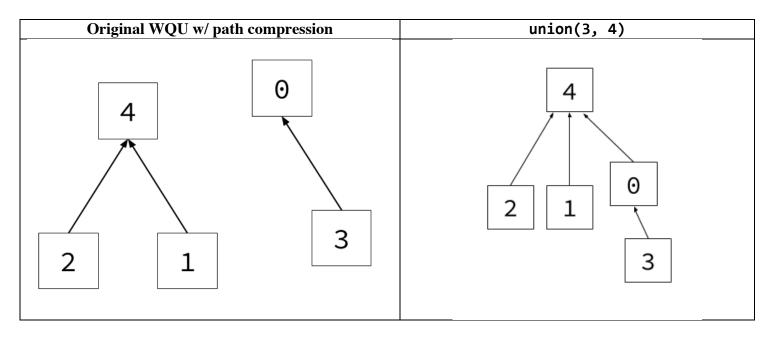
Original TST	List of Keys	insert("HOT")
B H H A A M T	BRR BURN HAM	B H A A R A T T T

Common Errors: Listing "BURR" as a key. Left and right children are NOT equal. Inserting 'o' as the right child of 'h' instead of 'a'. Not terminating nodes with "T"  $\rightarrow$  we need this in order to keep track of full words

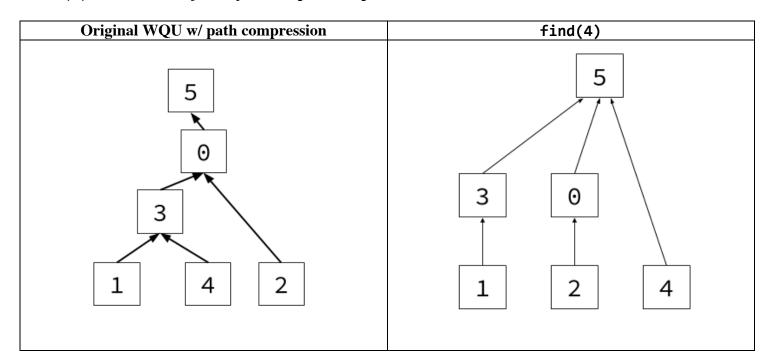
**b.** Consider the **binary min-heap** below. Draw the corresponding heap after removeMin() has been called once.



c. Consider the weighted quick union object below. In the space provided, draw the result of calling union(3, 4). Assume the object implements path compression.

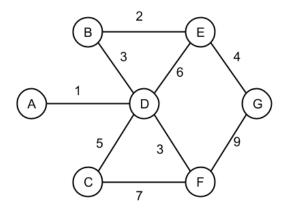


**d.** Consider the **weighted quick union** object below. In the space provided, draw the object after calling find(4). Assume the object implements **path compression**.



# 2. Changz (6 pts)

**a.** Consider the weighted undirected graph below. Write the order in which the vertices are visited using the specified algorithm. In the event of a tie, visit the vertices in alphabetical order. The starting vertex for each traversal is already written for you.



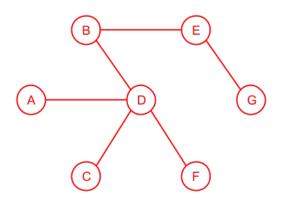
DFS: G E B D A C F

BFS: A D B C E F G

Dijkstra's: A D B F C E G

Common errors: For DFS, neighbors are visited alphabetically. For example, C should be visited before F when considering which neighbor to visit when at the D node.

**b.** For the same weighted undirected graph as in part **a**, draw the minimum spanning tree given by running Kruskal's algorithm. A blank graph has been provided below for your convenience. You need not include the edge weights.

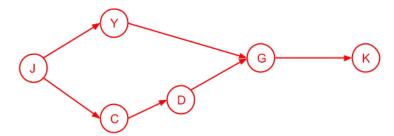


**c.** Suppose we wish to change the weights of the edges in the graph from part **a.** Is there an edge that will always be in the minimum spanning tree regardless of what its weight changes to? If so, write down the edge. If not, write *none exists*. No justification is necessary for either.

Yes, **A-D** will be in every MST of the graph.

**d.** Draw a directed graph that has **only** the following 3 topological sorts. Each vertex in your graph must be "touched" by at least one edge. That is, every vertex in your graph must have at least one edge either arriving or departing from it. There may be more than one answer. You only need to label your vertices with letters.

Topological Sort 1	Topological Sort 2	Topological Sort 3	
J. Go to Soda	J. Go to Soda	J. Go to Soda	
Y. Pair program	C. Ace the quiz	C. Ace the quiz	
C. Ace the quiz	Y. Pair program	D. Pull code to repo	
D. Pull code to repo	D. Pull code to repo	Y. Pair program	
G. Find bugs in code	G. Find bugs in code	G. Find bugs in code	
K. Pass the tests	K. Pass the tests	K. Pass the tests	



### Common errors:

- Not satisfying all topological sorts given
- Not having an edge from C-D (which allows for more topological sorts than given)
- Not drawing a directed acyclic graph

### **Chill-Out Corner**

Remember to breathe. Don't be afraid to chill with the Shadow below. He's nice. Draw him something. Steven suggests a Pusheen (reference on the left).





### 3. Aunty Tares (4 pts)

You've just been hired by a hot new DNA sequencing startup called *DAN'S DNA SHACK*. Your job is to build software that accepts full DNA sequences of length L and allows users to quickly check if certain DNA subsequences of varying length are present in the full sequence. Fill in the DNAMatcher class below so that its functionality matches its comments. The isSubsequence method should run in  $\Theta(R)$  time in the worst case and  $\Theta(1)$  time in the best case, where R is the length of the subsequence. There is no limit on the runtime of DNAMatcher's constructor. You may assume full will never be null.

Hint: You may find the Trie class helpful. You may also find helpful the String class' substring(int startIndex, int endIndex) method, which gets a String's substring from startIndex (inclusive) to endIndex (exclusive).

```
public class DNAMatcher {
    Trie t;
    /** Constructs a DNAMatcher object for a DNA sequence full. */
    public DNAMatcher(String full) {
        t = new Trie();
        for(int i = 0; i < full.length(); i++) {
            t.insert(full.substring(i, full.length()));
        }
    }
}

/**
    * Returns true if sub is a subsequence of the DNA sequence
    * given by full. Returns false otherwise.
    */
    public boolean isSubsequence(String sub) {
        return t.find(sub, false);
    }
}</pre>
```

#### Common errors:

- Only inserting full
- Off by one errors (substring's endIndex is exclusive)
- Not calling **find** on the trie instance.

# 4. Green Eggs and Sam (4 pts)

Consider the following unsorted array, and the same array after 4 iterations of insertion sort as discussed in lab and lecture (where we sweep through the array from left to right, and move an element to its *relative* correct position by swapping). The first iteration starts at index 1 (the second element in the array). <u>Assume no two elements are equal. Insertion sort arranges the elements from least to greatest.</u>

### **Unsorted:**



For each row, fill in the correct bubble **fully** that corresponds to the relationship between the symbols. If there is insufficient information to determine the relationship between two objects, fill in the ? bubble.

Symbol 1	<	>	?	Symbol 2
	0	0	•	
	0	•	0	
	•	0	0	

○ True / • False: • must be the smallest element in the array.

# 5. Lights Off Zeitsoff (4 pts)

**a.** We have regular expressions in the leftmost column of the table below. For each string, fill in the circle if the regular expression for that row fully matches that string.

For example, if the string **char** matches the regular expression (jar)\*migon, shade the bottom left box. Fill in the bubbles completely. If none of the strings match a given regular expression, leave that row blank.

	char	charmigon	jarmigon	charm	jar	migon	igon
charm	0	0	0		0	0	0
charm+	0	0	0		0	0	0
(char jar)migon	0	•	•	0	0	0	0
[charm]*igon	0	•	0	0	0		
(jar)*migon	0	0	•	0	0	•	0

For parts **b.** and **c.** write a regular expression that will fulfill the conditions below. Be sure to escape special characters. The regular expressions are **not** Java Strings.

b. Match a valid group repo name, where a repo name is the string "group" followed by at least one digit.

Fully matched inputs: "group17", "group200", "group000", "group0001" Non-matching inputs: "groups17", "", "17", "group"

Regex: group\d+

**c.** Match a valid US phone number. Match **only** the two formats shown below. **Hint:** "\s" matches a single whitespace.

```
Fully matched inputs: "(650) 123-6402", "408-244-1023"

Non-matching inputs: "1234567", "", "122-123", "12-123", "(65) 432-4596", "(65)-432-4596", "(6) 432-4596"
```

Regex:  $(\d{3}\)\s|\d{3}-\d{4}$ 



## 6. Some-Ting Wrong (4 pts)

For each of the methods below, bound the <u>overall</u> runtime of the method using Big-Theta notation in terms of the input N. If not possible, write "N/A". For full credit, your answer should be as simple as possible with no unnecessary leading constants or lower order terms.

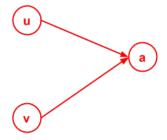
```
\Theta(N^3)
             private static void f(int N) {
                 for (int i = 0; i < N; i++) {
                      for (int j = 0; j < N; j++) {
                          linear(N); // runs in linear time with respect to input
                      }
                 }
             }
N/A
             private static void g(int N) {
                   if (N < 1) return;
                  for (int i = 0; i < N; i++) {
                       g(100);
                   }
                  g(N/2);
                  g(N/2);
              }
Intent of the question was for \Theta(N \lg N), but we messed up.
N/A
          private static void h(int N) {
              Random generator = new Random();
              for (int i = 0; i < N; i++) {
                 if(generator.nextBoolean()) { // returns true with probability .5
                      break;
                  }
              }
          }
\Theta(lg \ N \ lg \ (lg \ N)) public static void i(int N) {
                     TreeSet<Integer> t = new TreeSet<>(); // Uses a Red-Black Tree
                     for (int i = N; i > 0; i /= 2) {
                         t.add(i);
                     }
                 }
```

# 7. A Supposedly Fun Ching I'll Never Do Again (8 pts)

- a. Which of the following types of graphs always have a topological sort?
- Non-circular singly linked list
- Binary search tree with no parent pointers
- ☐ Undirected cyclic graph
- Directed acyclic graph
- ☐ Connected graph
- **b.** For each of the following, indicate whether the statement is true or false. If true, provide a **brief** 1-2 sentence justification. If false, provide a graph as a counterexample.
- True /  $\bigcirc$  False: Suppose we run Dijkstra's algorithm on a graph G, starting from vertex v. If the only negative edges in G are outgoing edges from v (and there are no negative cycles), then Dijkstra's will be able to find the shortest-paths from v.

Dijkstra's just needs the guarantee that, as paths are expanded, the costs increase. If the only negative edges are around the start vertex, then there is not chance for some path to decrease in cost further into the expansion.

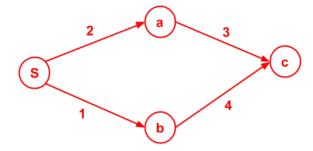
 $\bigcirc$  True /  $\bigcirc$  False: Suppose we topologically sort some graph G. If vertex u is the first item in the sort, then for some other vertex v in the sort, we know there is a path from u to v in G.



Consider a graph with two source vertices. (Must specify source vertices)

 $\bigcirc$  True /  $\bigcirc$  False: Given a graph **G** with unique edge weights, the shortest paths from some start vertex **s** to all other vertices are unique.

In the graph below, there are two shortest paths from s to c,  $s \rightarrow a \rightarrow c$  and  $s \rightarrow b \rightarrow c$ .



True /  $\bigcirc$  False: Suppose you want to run breadth-first search and Dijkstra's algorithm on a graph G, whose edge weights are all the same positive number. Assuming the two algorithms make the same tie-breaking choices, the order in which nodes will be polled from the BFS queue is the same as the order in which nodes will be polled from the priority queue of Dijkstra's algorithm.

In the particular case where all the edge weights are length one, the shortest distance from a node to the start node in Dijkstras corresponds to the number of edges between the node to the start node, which is the search order for BFS. For larger edge weights, the numbers are simply scaled down to the length one case.

**c.** We are trying to find the minimum spanning tree (MST) of a graph where the edge weights may range between 0 and 255. Christine suggests that it is possible to find the MST in a time faster than  $O(|E| \lg |E|)$ . Is this true? If so, **briefly** explain how can this be done. If not, **briefly** explain why.

True because we can use radix sort in order to sort the edges.

**d.** Steven needs to find the shortest path from his home to a Pusheen Conference. Let us define a graph G where there are |V| vertices representing different locations, and |E| edges representing the distances between locations. Steven's home is represented by the start vertex s, while the Pusheen Conference location is represented by the target vertex t. Steven will need to make one stop for gas on his route from s to t. These gas stations are represented by an *array* of vertices. For example, the array  $[g_1, g_2, ..., g_n]$  indicates that there are n gas station locations.

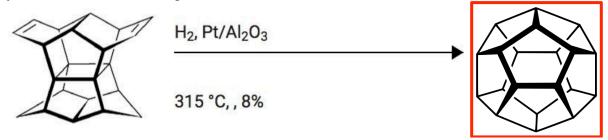
Consider how one would write an algorithm that would find the shortest path from s to t such that at least one gas station is on the path. Describe how your algorithm would work in 3-4 sentences. For full credit, your algorithm should run in  $O((|V| + |E|) \lg |V| + n)$ . We will give partial credit to algorithms that provide the correct solution, but run in slower time. You must provide your algorithm's runtime.

Run Dijkstra's from **s** and then run Dijkstra's from **t**. Afterwards, go through  $[g_1, g_2, ..., g_n]$ . For each  $g_i$ , sum the cost of the path from **s** to  $g_i$  and the path from  $g_i$  to **t**. Return the minimum path.

Runtime:  $O((|V| + |E|) \lg |V| + n)$ .

#### **0. PNH**

What is the name of the simplest hydrocarbon with full icosahedral symmetry? The final reaction step to synthesize this molecule is provided below.



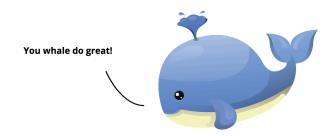
Dodecahedrane

### 8. JC and the Whale Pod (3 pts)

You are given a list of **unsorted** sublists containing **Comparable** elements. Using streams, complete the method below to sort the **unsorted** sublists and combine them into one final list containing all the sorted elements. If 1st is empty, return an empty LinkedList.

#### Common Errors:

- Forgetting reduce is a terminal operation and calling collect after
- Calling orElse(null) after reduce instead of orElse(new LinkedList<T>()), or forgetting orElse altogether!
- Calling methods after forEach. forEach is a terminal operation and returns void
- map takes in a lambda function of only one argument! Many tried to pass in two arguments



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Gigi and Diana encourage you to continue.

## 9. Big Baller Alex (6 pts)

Consider an undirected graph representing social relationships, where vertices represent people and edges represent connections. Person A and Person B are considered to be in the same network if a path exists in the graph from Person A's vertex to Person B's vertex. Implement the constructor and methods of the SocialNetworks class, which models these social relationships. You may assume everything on the reference sheet is imported.

A series of y isSameNetwork and x addConnection calls should run in  $\Theta(x + y \cdot \alpha(x + y, x))$ .

```
public class SocialNetworks {
    UnionFind uf;
    HashMap<String, Integer> nameToID;

/**
    * Initializes a social graph initialized with users.size() people
    * whose names are stored in users.
    */
public SocialNetworks(Set<String> users) {
        uf = new UnionFind(users.size());
        nameToID = new HashMap<>();
        int ID = 0;
        for (String user : users) {
            nameToID.put(user, ID);
            ID++;
        }
    }
}
```



```
... (continued on next page) Chirithy says to follow your dreams
```

```
* Returns true if the users with names n and o are valid and in the
 * same network. Otherwise, returns false.
public boolean isSameNetwork(String n, String o) {
    if (!nameToID.containsKey(n) || !nameToID.containsKey(o)) {
       return false;
    return uf.isConnected(nameToID.get(n), nameToID.get(o));
}
 * If n and o are names of valid users, add a connection between
 * them if such a connection doesn't exist already.
 * Does not modify the SocialNetwork if n or o are not valid names.
public void addConnection(String n, String o) {
    if (!nameToID.containsKey(n) | !nameToID.containsKey(o)) {
        return;
    uf.union(nameToID.get(n), nameToID.get(o));
}
public static void main(String[] args) {
    Set<String> users = new HashSet<>();
    users.add("Matt Owen");
    users.add("Alison Tanubrata");
    users.add("Wayne Li");
   SocialNetworks mySpace = new SocialNetworks(users);
   mySpace.addConnection("Matt Owen", "Alison Tanubrata");
   System.out.println(mySpace.isSameNetwork("Matt Owen",
                      "Alison Tanubrata")); // Should print true!
   System.out.println(mySpace.isSameNetwork("Matt Owen",
                      "Wayne Li")); // Should print false!
```

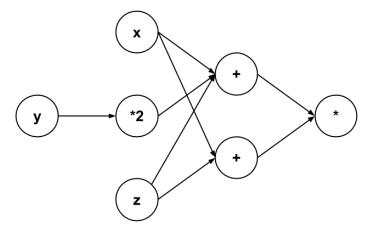
```
UC BERKELEY
Class ID:
    }
}
```

#### Common errors:

- Only accounting for direct connections/not using the UnionFind structure
- Not giving unique ID for each new user
- Calling contains instead of containsKey in HashMap calls
- Forgetting to initialize HashMap in the constructor!

### 10. Matt Sit Down, Be Humble (7 pts)

A computational network is a way to graphically model a mathematical function. For instance, given the function f(x, y, z) = (x + 2 \* y + z) \* (x + z), the corresponding computational network would look as follows:



There are three kinds of nodes in a computational network: InputNodes, which represent variables and the value they take on, MapperNodes, which take the output of one node and maps it to a different value through its Function's apply method, and CombinerNodes, which can take an arbitrary number of inputs and combine them together through its BinaryOperator's apply method. Complete the code on the following pages such that the main method works as specified and your implementations match the behavior described in the comments.

Hint: You will need to use streams.

```
import java.util.Arrays;
import java.util.List;
import java.util.function.BinaryOperator;
import java.util.function.Function;
public class CompNet {
    private List<InputNode> input;
    private Node output;
    private interface Node {
        public double visit();
```

```
}
   /** Sets the InputNodes for this CompNet. */
   public void setInputNodes(List<InputNode> lst) { ... }
    /** Sets the output Node for this CompNet. */
   public void setOutputNode(Node node) { ... }
... (continued on next page)
   /** Creates the CompNet described in the picture on the previous page. */
   public static void main(String[] args) {
       CompNet c = new CompNet();
        InputNode x = new InputNode(-2.0);
        InputNode y = new InputNode(5.0);
        InputNode z = new InputNode(-4.0);
       MapperNode times2 = new MapperNode(y, (a) -> a * 2);
       CombinerNode add = new CombinerNode(
                Arrays.asList(x, times2, z), (a, b) \rightarrow a + b;
       CombinerNode secondAdd = new CombinerNode(Arrays.asList(x, z),
                (a, b) \rightarrow a + b);
       CombinerNode mult = new CombinerNode(Arrays.asList(add, secondAdd),
                (a, b) -> a * b);
        c.setOutputNode(mult);
       System.out.println(c.compute()); // Should print out -24.0
   }
   /** Returns the computation that this CompNet represents. */
   public double compute() {
        return output.visit();
   }
     * A Node in a CompNet that represents a variable and the
     * value it takes on.
     * Returns its value upon being visited.
   private static class InputNode implements Node {
        private double value;
        public InputNode(double value) { ... }
       public double visit() {
            return value;
        }
    }
```

- Need to implement Node (not extend) and override the visit method.
- You cannot return anything when inside a class and not inside a method.

```
... (continued on next page)
    /**
    * A Node in a CompNet that combines the result of its inputs
    * through its BinaryOperator upon being visited.
    * The order in which inputs are combined does not matter.
    * If input is length 1, return the result of that one Node.
    * If input is input of length 0, return 0.0
    */
   private static class CombinerNode implements Node {
       List<? extends Node> input;
       BinaryOperator<Double> combiner;
        public CombinerNode(List<? extends Node> input,
                            BinaryOperator<Double> combiner) { ... }
        public double visit() {
            return input.stream().map(Node::visit).reduce(combiner).orElse(0.0);
        }
    }
```

#### Common Errors:

- Forgetting a call to map, forgetting a call to reduce, forgetting to handle the Optional at the end of the reduce call
- Accessing .value directly from the Node, not all Nodes have a value!
- Extraneous if cases that forced you to use more lines than necessary.
- Writing extends instead of implements
- Not overriding visit() (which has to be public and has to return a double)

```
/**
 * A Node in a CompNet that maps the result of its input
 * through its Function upon being visited.
 */
private static class MapperNode implements Node {
    private Node input;
    private Function<Double, Double> mapper;
    public MapperNode(Node input, Function<Double, Double> mapper) { ... }
    public double visit() {
        return mapper.apply(input.visit());
}
```

```
}
}
}
```

#### Common errors:

- extends Node instead of implements Node
- Did not call input.visit()
- Attempted to use streams incorrectly e.g. used input.toStream()

This is a Chim Chim.



### 11. Christine the Coding Machine (10 pts)

The *k*-nearest neighbors problem is defined as follows. Given a set of N points and a query Point q, output the k points closest to q.

**a.** Complete the following method that finds the k-nearest neighbors by scanning through the input array, and keeping track of the k nearest points. The outputted array should be ordered with the closest point at index 0 and the farthest point at index k-1. The code should run in  $\Theta(N \lg k)$  time in the worst case, where N is the length of arr.

```
import java.util.PriorityQueue;
/** Returns the distance between a and b. */
private static int dist(Point a, Point b) { ... }
public static Point[] slowKNN(Point[] arr, Point q, int k) {
    PriorityQueue<Point> pq = new PriorityQueue<>((a,b) ->
                                  dist(q, b) - dist(q, a));
    for (Point p : arr) {
        pq.add(p);
        if (pq.size() > k) {
            pq.poll();
        }
    }
    Point[] neighbors = new Point[k];
    for (int i = k - 1; i >= 0; i--) {
        neighbors[i] = pq.poll();
    return neighbors;
}
```

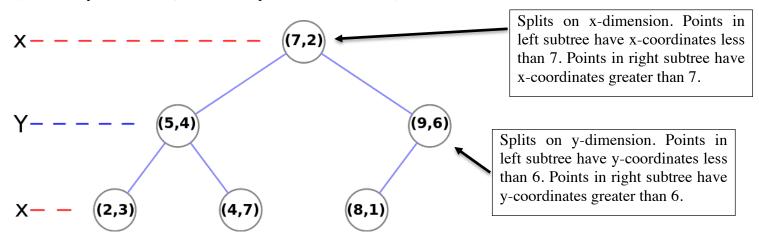
#### Common errors:

- Creating a PriorityQueue with no Comparator
- Writing an  $\Theta(N \lg N)$  solution (exam asks for a  $\Theta(N \lg k)$  solution)
- Having the reversed Comparator: (a,b) -> dist(q, a) dist(q, b)

**b.** You can complete this part without having done part **a**. A *k-d tree* is a data structure specialized for storing points. It can be used to optimize the k-nearest neighbors query.

More specifically, a k-d tree is a binary tree, where each node in the tree contains a point of dimension k. Each node stores the dimension it splits on (to determine how to divide the rest of the points). At each level of the tree, we will cycle through the dimensions, splitting on a different dimension for each level.

For example, given the point set [(2, 3), (5, 4), (9, 6), (4, 7), (8, 1), (7, 2)], (2 dimensional points), the corresponding k-d tree will look like below. First, we split on the x-dimension (which corresponds to dimension 0), then the y-dimension (which corresponds to dimension 1), and so forth.



Given an array of Points, we can recursively build up a balanced k-d tree with the following algorithm: At each level of recursion, we will find the median of the Point array based on the dimension index. We will create a new node containing that Point. Afterwards, we will recurse on all the Points before the median point, splitting on the next dimension, setting the results to be the left child. We do the same for the points after the median.

Complete the code below to construct a KDTree that stores the array of Points given by arr.

```
import java.util.PriorityQueue;
public class Point { ... }
public class KDTree {
    private TreeNode root;
    private int dim;
```

```
private class TreeNode {
       Point item;
       TreeNode left;
       TreeNode right;
        int depth;
        private TreeNode(Point item, int depth,
                         TreeNode left, TreeNode right) {...}
   }
... (continued on next page)
   public KDTree(Point[] arr, int d) {
       dim = d:
       root = buildTree(arr, 0);
   }
    /**
     * Returns the i-th largest Point in arr based on the dimIndex-th dimension.
     * Partitions and modifies arr in-place accordingly.
     * Points less than the i-th largest will be to the left of index i.
     * Points greater than the i-th largest will be to the right of index i.
     * dimIndex must be between 0 and dim - 1.
   private static Point partition(Point[] arr, int i, int dimIndex) { ... }
   /** Recursively builds a k-d tree. */
   public TreeNode buildTree(Point[] arr, int depth) {
        if (arr.length == 0) {
            return null;
        } else {
            Point median = partition(arr, arr.length / 2, depth % this.dim);
            Point[] before = new Point[arr.length / 2];
            Point[] after = new Point[arr.length - arr.length / 2 - 1];
            for (int i = 0; i < before.length; i++) {</pre>
                before[i] = arr[i];
            }
            for (int i = 0; i < after.length; i++) {</pre>
               after[i] = arr[arr.length / 2 + i + 1];
            }
```

```
TreeNode left = buildTree(before, depth + 1);
    TreeNode right = buildTree(after, depth + 1);
    return new TreeNode(median,depth, left, right);
}
}
```

**c.** You can complete this part without having done part **b**. To perform a k-nearest neighbors query, we will search through the k-d tree in a manner similar to how you traversed your trie or TST in Autocomplete.

A TreeNode represents a bounding box in space (don't worry too much about it). We will keep a fringe of TreeNodes to visit, ordered by the distance from the query point to the bounding box that the TreeNode represents, calculated through the dist method below. We will also keep a PriorityQueue to keep track of the current nearest Points we have. In order to not have to explore the entire tree, we will only push TreeNodes onto the fringe if we still have not put k Points in the PriorityQueue OR the distance from the query point to the TreeNode is less than the distance from the query point to the kth farthest Point in the PriorityQueue.

On the next page, complete the kNN method of the KDTree class below. The resulting array should be ordered with the closest point at index 0 and the farthest point at index k - 1. Assume there will always be at least k points in the k-d tree. Assume that all points in the KDTree have a unique distance from the query point.

**Hint:** Don't forget null checks

```
import java.util.PriorityQueue;
public class Point { ... }
public class KDTree {
    private TreeNode root;
    private int dim;
    ...
    /** Returns the distance between q and the bounding box represented by a. */
    private static int dist(Point q, TreeNode a) { ... }
    /** Returns the distance between a and b. */
    private static int dist(Point a, Point b) { ... }
```

### Common errors:

- Forgetting to add root to the fringe
- Adding TreeNodes to top, when it's a PriorityQueue of Points
- Not null checking
- Adding extraneous TreeNodes to the fringe
- Comparing the TreeNode popped off from the fringe instead of its children (its children could be closer)
- Iterating forwards to fill in the return array



```
Chao chao!
... (continued on next page)
    public Point[] kNN(Point q, int k) {
        PriorityQueue<TreeNode> fringe = new PriorityQueue<>((a, b) ->
                                               dist(q, a) - dist(q, b));
        PriorityQueue<Point> top = new PriorityQueue<>((a,b) ->
                                         dist(q, b) - dist(q, a));
        fringe.add(root);
        while (!fringe.isEmpty()) {
            TreeNode node = fringe.poll();
            Point p = node.item;
            top.add(p);
            if (top.size() > k) {
                top.poll();
            }
            int closest = dist(q, top.peek());
            if (node.left != null &&
                     (pq.size() < k || dist(q, node.left) < closest)) {</pre>
                fringe.add(node.left);
            }
            if (node.right != null &&
                     (pq.size() < k || dist(q, node.right) < closest)) {</pre>
                fringe.add(node.right);
            }
        }
```

```
UC BERKELEY
Class ID: ____
```

```
Point[] neighbors = new Point[k];
for (int i = k - 1; i >= 0; i--) {
    neighbors[i] = pq.poll();
}
return neighbors;
}
That's it! Thank yo
```



That's it! Thank you for an awesome summer! ©