# Physics 7C, Spring 2014 Instructor: Professor Adrian Lee 

Midterm Examination, Tuesday, February 25, 2014
Please do work in your blue/greenbooks. Show your reasoning carefully so that we can be sure that you derived the answer rather than guessing it or relying on memory; in addition, this enables us to give partial credit. You may use one double-sided $3.5 \times 5$ index cards of notes. You can use a simple calculator (no smart phones or devices that can store notes). Test duration is 110 minutes.

## 1 Qualitative Questions [30 pts. total]

Only a few lines of explanation is needed for these. You don't have to use cartoons or equations, unless specified, but you can. No derivations are needed.
a) If you have a bare optical fiber made of glass $(n=1.2)$, can you get total internal reflection with the fiber in water $(\mathrm{n}=1.33)$ ? [5 pts.]
b) If a concave spherical mirror produces a real image, can it be upright only, inverted only, or both compared to the original object? You probably need ray diagram(s) for this question. [5 pts.]
c) For an electric field $E=E_{0} \sin (k x-\omega t) \hat{y}$ what is its velocity include the correct sign? [ 5pts.]
d) If you reverse a lens (flip it around the vertical), does it act the same and have the same focal length? [5 pts]

## 2 Reimaging System [30 pts. total]



A small arrow is a distance $d_{1}$ from a diverging lens as shown in the figure. A converging lens with a focal length $f_{c}$ is a distance $d_{2}$ to the right of the diverging lens with a focal length $f_{d}$. The two lens system forms a real inverted image a distance $d_{3}$ to the right of the converging lens. You should assume that $d_{2}>f_{c}, d_{2}>f_{d}$ and $d_{2}>\left|f_{c}\right|+\left|f_{d}\right|$.
a) Draw a ray diagram [10 pts.]
b) Find an expression for the focal length of the diverging lens $f_{d}$ in terms of $d_{1}, d_{2}, d_{3}$ and $f_{c}$. [10 pts.]
c) What is the magnification of the optical system? You can use any of the variables in the problem $f_{d}, f_{c}, d_{1}$, $d_{2}$ and $d_{3}[10 \mathrm{pts}$.]

## 3 Space Telescope [30 pts. total]



A telescope for space observations consists of two spherical mirrors arranged as shown in the figure. The large primary and small secondary mirrors have radii equal to $R$ and $r$ respectively. The distance between the mirrors is $D$ and $D<R / 2$. You can also assume that the secondary mirror is positioned such that the final image is formed as shown in the figure. This telescope design is called a "Maksutov Cassegrain."
a) Make a ray diagram showing where the final image is for an object at $d_{o}=$ infinity. Is the image of the primary real or virtual? Is the object for the secondary real or virtual? [ 15 pts .]
b) What is the distance from the primary mirror to the final image? [ 15 pts .]

## 4 Solar Sail [30 pts. total]

A small perfectly reflecting sail of area $A$ is a distance $D$ away from the sun, with $A \ll D^{2}$. The amount of energy absorbed by the sail during a time interval $T$ is measured to be $U_{a b s}$. In terms of these quantities, please answer the following:
a) What is the amplitude of the electric field incident on the sail coming from the sun, $E_{0}$ ? [10 pts.]
b) What is the power output of the sun, assuming it radiates uniformly in all directions? [10 pts.]
c) In some coordinate system, the electric field incident on the sail can be written $E_{\text {in }}=E_{0} \sin (k x-\omega t) \hat{y}$. Write the magnetic field in terms of these quantities. [10 pts.]
d) In this same coordinate system, what possible directions could the electric field have been pointing if it was not pointing in the $\hat{y}$ direction? The propagation direction can not change. Possibilities include the $\hat{x}$ and/or $\hat{z}$ directions. [5 pts.]
e) Could the electric field be written $E_{i n}=E_{0} \sin \left(k x-\omega t^{2}\right) y$ ? [5 pts.]

