Physics 7b
Fall 2006
Midterm 1
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Work all problems. Introduce and clearly define algebraic symbols to represent all physical quantities. Do not perform numerical work until you have a final algebraic answer within a box. Check the dimensions of your answer before inserting numbers. Work the easiest parts first, and the next hardest, etc. If you do not understand the question ask the proctor for assistance. All problems are weighted equally.
$\mathrm{k}_{\mathrm{B}}=1.38 \times 10^{-23} \mathrm{~J} / \mathrm{K}, \mathrm{N}_{\mathrm{A}}=6.02 \times 10^{23}$, latent heat of fusion of water $3.3 \times 10^{5} \mathrm{~J} / \mathrm{kg}$, specific heat of ice, $2100 \mathrm{~J} / \mathrm{kgC}^{0}$, specific heat of liquid water $4186 \mathrm{~J} / \mathrm{kgC}^{\circ}$, $\sigma=5.6 \times 10^{-8} \mathrm{~W} / \mathrm{m}^{2} \mathrm{~K}^{4}$

When considering gas processes you may assume the gas follows the ideal gas law.

Name $\qquad$
SID $\qquad$
Sect. \# or day and time $\qquad$
TA name (if known)

1. $\qquad$
2. $\qquad$
3. $\qquad$
4. $\qquad$
5. $\qquad$

Total $\qquad$

## Problems 1,2, and 3 all are based on the same "house" described in problem 1.



1. Consider a house with a square "footprint" (i.e. base) 10 m on each side and height 5 m . Air is $\sim 80 \% \mathrm{~N}_{2}$ with a molecular weight $\mathrm{M}_{\mathrm{w}}=28 \mathrm{~g} / \mathrm{mole}$
a. (5pts) Estimate how many air molecules fill the interior space of the house when the inside temperature is $20^{\circ} \mathrm{C}$. Tell what assumptions you made for the estimate.
b. (5pts) The walls of the house have a linear expansion coefficient $\alpha=1 \times 10^{-5} /{ }^{\circ} \mathrm{C}$. If the temperature of the walls changes by $10^{\circ} \mathrm{C}$, what is the fractional change in the interior volume?
c. (5pts) Assuming that the house is not air tight, what is the fractional change in the number density of molecules (i.e. number per unit volume) corresponding to this $10^{\circ} \mathrm{C}$ temperature rise.?
2. a. (5pts) When the inhabitants of the house go away on vacation they turn off the heat. When they return they turn it back on. How many kWhrs of energy does it take to raise the temperature of the air in the house by $15^{\circ} \mathrm{C}$ ? Ignore heat losses during the warm up time. Express your answer in terms of a numeric factor times the symbol N , which will stand for the answer in problem 1a above.
b. (5pts) If the house heater output is 5 kW , how long does it take to raise the temperature by those $15^{\circ} \mathrm{C}$ ? Again, use the symbol N to stand for the answer in problem 1a.
3. (15pts) This house requires 5 kW of heat on a winter day when it is $13^{\circ} \mathrm{C}$ outside and $21^{\circ} \mathrm{C}$ inside. In the summer this house is cooled by an air conditioner (a refrigerator unit which cools the inside, pumping the heat to the outside) which operates at $75 \%$ of the Carnot coefficient of performance for a refrigerator. When it is $37^{\circ}$ outside, how much does it cost to cool the house for one month if the inside temperature remains at $21^{\circ} \mathrm{C}$ inside and if the cost of electricity is $\$ 0.14 / \mathrm{kWhr}$. Assume the inside and outside temperatures remain constant.
4. ( 15 pts ) A metal ball of radius 1 m is heated to a temperature of $800^{\circ} \mathrm{C}$. The ball is placed near a curved mirror so that $20 \%$ of the emitted thermal radiation falls onto a small box containing 5 kg of ice at $-10^{\circ} \mathrm{C}$. Assuming the ball's emissivity is $\varepsilon=0.6$ and the absorptivity of the box is 1 , how long does it take to melt the ice and raise the water within to $+20^{\circ} \mathrm{C}$ ?

5. (15pts) (Prob. 20-39 from homework) What is the total change in entropy when 2.5 kg of water at $0^{\circ} \mathrm{C}$ is frozen to ice at $0^{\circ} \mathrm{C}$ by being in contact with 450 kg of ice at $-15^{\circ} \mathrm{C}$ ?
