### INSTRUCTIONS

- You have 45 minutes to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except one hand-written 8.5” × 11” sheet of notes of your own creation and the official midterm exam reference guide provided with the exam.
- Mark your answers **on the exam itself**. We will *not* grade answers written on scratch paper.

| Last name          |  
|--------------------|------|
| First name         |  
| Student ID number  |  
| BearFacts email    | `@berkeley.edu` |
| GSI                |  
| Name of the person to your left |  
| Name of the person to your right |  

*All the work on this exam is my own.*

(please sign)
1. **(16 points) Expressions**

A table named `pay` contains one row for each UC Berkeley faculty member and these columns:

- **dept**: a string, the department of the faculty member.
- **name**: a string, the first name of the faculty member.
- **role**: a string, one of: Assistant Professor, Associate Professor, Professor, or Lecturer
- **salary**: an int, last year’s salary paid by the university.

<table>
<thead>
<tr>
<th>dept</th>
<th>name</th>
<th>role</th>
<th>salary</th>
</tr>
</thead>
<tbody>
<tr>
<td>Journalism</td>
<td>Jeremy</td>
<td>Lecturer</td>
<td>111,528</td>
</tr>
<tr>
<td>Economics</td>
<td>Christina</td>
<td>Professor</td>
<td>349,727</td>
</tr>
<tr>
<td>South &amp; Southeast Asian Studies</td>
<td>Penelope</td>
<td>Associate Professor</td>
<td>127,119</td>
</tr>
</tbody>
</table>

... (2056 rows omitted)

**Fill in the blanks of the Python expressions to compute the described values.** You must use *all and only* the lines provided. The last (or only) line of each answer should evaluate to the value described. Assume that the statements `from datascience import *` and `import numpy as np` have been executed.

(a) **(2 pt)** The total salary amount paid to all faculty.

```python
------------------(pay.____________________________(______________________________________________))
```

(b) **(3 pt)** The name of the third highest paid faculty member. (Assume no two faculty have the same salary.)

```python
pay._________(_________ , _____________________________).column(_________).item(_________)
```

(c) **(3 pt)** The number of lecturers in the department that has the most lecturers. (One has more than the rest.)

```python
max(pay._________(_________ , ___________________)._________(____________).column('count'))
```

(d) **(3 pt)** The average faculty salary after all faculty members get a 10% raise each year for three years.

```python
__________________________________________________________________________________________
```

(e) **(5 pt)** The table `big` (created below) only contains rows for faculty in departments that have both Lecturers and Professors. Using `big`, compute the minimum pay gap for any department. The pay gap is the absolute difference between a department’s average Lecturer salary and its average Professor salary.

```python
has_lecturer = pay.pivot('role', 'dept').where('Lecturer', are.above(0))
has_both = has_lecturer.where('Professor', are.above(0))
big = pay.where('dept', arecontained_in(has_both.column('dept')))

avg = big._________(____________ , ______________ , ______________ , ______________)

------------------(avg.column(______________) == avg.column(______________)))
```
2. (14 points) Distributions

Galton measured the heights of the members of 200 families that each included 1 mother, 1 father, and some varying number of adult sons. The three histograms of heights below depict the distributions for all mothers, fathers, and adult sons. All bars are 2 inches wide. All bar heights are integers. The heights of all people in the data set are included in the histograms.

(a) (8 pt) Calculate each quantity described below or write Unknown if there is not enough information above to express the quantity as a single number (not a range). Show your work!

i. The percentage of mothers that are at least 60 inches but less than 64 inches tall.

ii. The percentage of fathers that are at least 64 but less than 67 inches tall.

iii. The number of sons that are at least 70 inches tall.

iv. The number of mothers that are at least 60 inches tall.

(b) (2 pt) If the father’s histogram were redrawn, replacing the two bins from 72-to-74 and from 74-to-76 with one bin from 72-to-76, what would be the height of its bar? If it’s impossible to tell, write Unknown.

(c) (4 pt) The percentage of sons that are taller than all of the mothers is between _________ and _________. Fill in the blanks in the previous sentence with the smallest range that can be determined from the histograms, then explain your answer below.
3. (12 points) Probability

(a) (3 pt) A basket of 10 colored tickets contains 1 blue, 1 gold, 4 green, and 4 red tickets. If you draw 6 tickets uniformly at random with replacement, what is the chance that you draw at least one that is either blue or gold? Write your answer as a Python expression that computes the result exactly (no simulation).

(b) (5 pt) The roll function draws an empirical histogram of the number of results that are \( k \) or larger, when \( n \) fair 6-sided dice are rolled. For example, if \( k \) is 5, \( n \) is 3, and rolling 3 dice results in a 6, a 4, and a 5, then 2 of the 3 dice are 5 or larger (the 6 and the 5). Fill in the blanks to complete its implementation.

```python
def roll(k, n, trials):
    """Repeatedly roll n dice and check how many results are k or larger."""
    outcomes = make_array()
    possible_results = ____________________________
    for i in np.arange(trials):
        rolls = np.random.choice(possible_results, ___________________)
        outcomes = np.append(________, np.count_nonzero(____________))
    Table().with_column('Outcomes', outcomes).hist(bins=np.arange(30))
```

(c) (4 pt) For each of the histograms below, circle the letter of the expression that generated it, assuming roll is implemented correctly above.

Circle one:  
(A) roll(4, 30, 5000)  
(B) roll(6, 30, 5000)  
(C) roll(4, 30, 50)  
(D) roll(6, 30, 50)  

Circle One:
(A) roll(4, 30, 5000)  
(B) roll(6, 30, 5000)  
(C) roll(4, 30, 50)  
(D) roll(6, 30, 50)
4. (8 points) Hypothesis Testing

A recent paper called *Do animals bite more during a full moon?* analyzed 1,660 emergency room visits for animal bites over a two-year period. The table shows bite counts by the day of the lunar cycle. In the lunar cycle, the moon is full on days 29, 30, and 1. On all other days, the moon is not full.

<table>
<thead>
<tr>
<th>Day</th>
<th>17, 18, 19</th>
<th>20, 21, 22</th>
<th>23, 24, 25</th>
<th>26, 27, 28</th>
<th>29, 30, 1</th>
<th>2, 3, 4</th>
<th>5, 6, 7</th>
<th>8, 9, 10</th>
<th>11, 12, 13</th>
<th>14, 15, 16</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bites</td>
<td>136</td>
<td>151</td>
<td>162</td>
<td>202</td>
<td>268</td>
<td>154</td>
<td>141</td>
<td>145</td>
<td>147</td>
<td>154</td>
</tr>
</tbody>
</table>

(a) (4 pt) Fill in the blanks of this null hypothesis so that it can be tested using the data above and so that it would help inform the question of whether there is a relation between bite frequency and the full moon.

The day of the lunar cycle on which an animal bites is drawn ____________________________, so the _____________________________ that an animal will bite on days 29, 30, and 1 of the lunar cycle is ______________. Any deviation from this proportion is due to ___________________________.

(b) (4 pt) The histogram below shows the empirical distribution of a test statistic under the null hypothesis. It was generated by repeating the following process 1000 times: the lunar day for each of 1660 simulated animal bites was chosen uniformly at random from 1 to 30. A test statistic was computed for each resulting list of 1660 days: the absolute difference between \( \frac{1}{10} \) and the proportion of bites on days 29, 30, and 1.

(Note: The proportion of observed bites on lunar days 29, 30, and 1 was \( \frac{268}{1660} = 0.161 \).)

Fill in each blank in the conclusion below:

We ______________ the null hypothesis because the observed value of the ______________ is ______________, which is ______________ with the null distribution.

(a number)