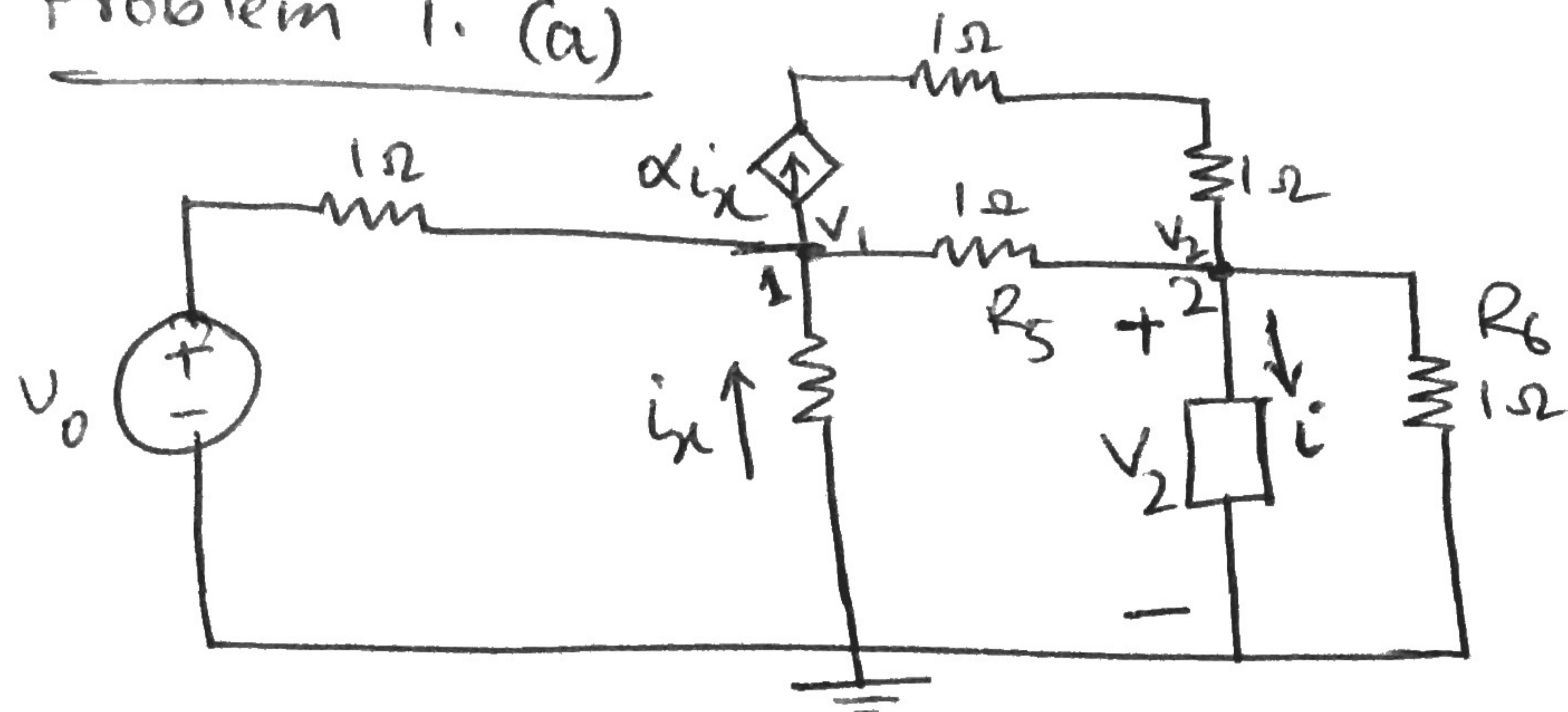


Problem 1. (a)



To Find  $i_x$  and hence  $i$ , we can any of the given  $V_0$  conditions, for simple calculation.

I am using  $V_0 = 2V$  condition, ( $V_0 = 1$  condition will give same result).

$$\text{So, } V_1 = -1V, V_2 = -5V$$

$$\therefore i_x = \frac{0 - (-1)}{1} = 1A$$

Now, KCL at node 2,

$$\frac{V_2 - V_1}{R_5} + \frac{V_2}{R_6} - \alpha i_x + i = 0$$

$$\Rightarrow 2V_2 - V_1 - \alpha i_x + i = 0$$

$$\Rightarrow i = \alpha i_x - 2V_2 + V_1$$

$$= 10 - 10 - 1$$

$$= -1A$$

Let's find the element inside the box:

~~Cathode~~ Current is going from negative to the positive potential. So, it must be an active

Source and not a passive element (e.g. resistor).

Can it be an <sup>independent</sup> voltage source?

- NO.  $V_2$  varies with  $V_o$ .

Can it be a dependent voltage source?

- NO.

| say, the element is a VCVS,  $V_{box}$ .  
~~then, for  $V_o \neq 0$~~  so,  $V_{box} = \beta V_o$ .

$$\text{If } V_o = 1, \beta = \frac{16}{5}$$

$$\text{If } V_o = 2, \beta = 2.5$$

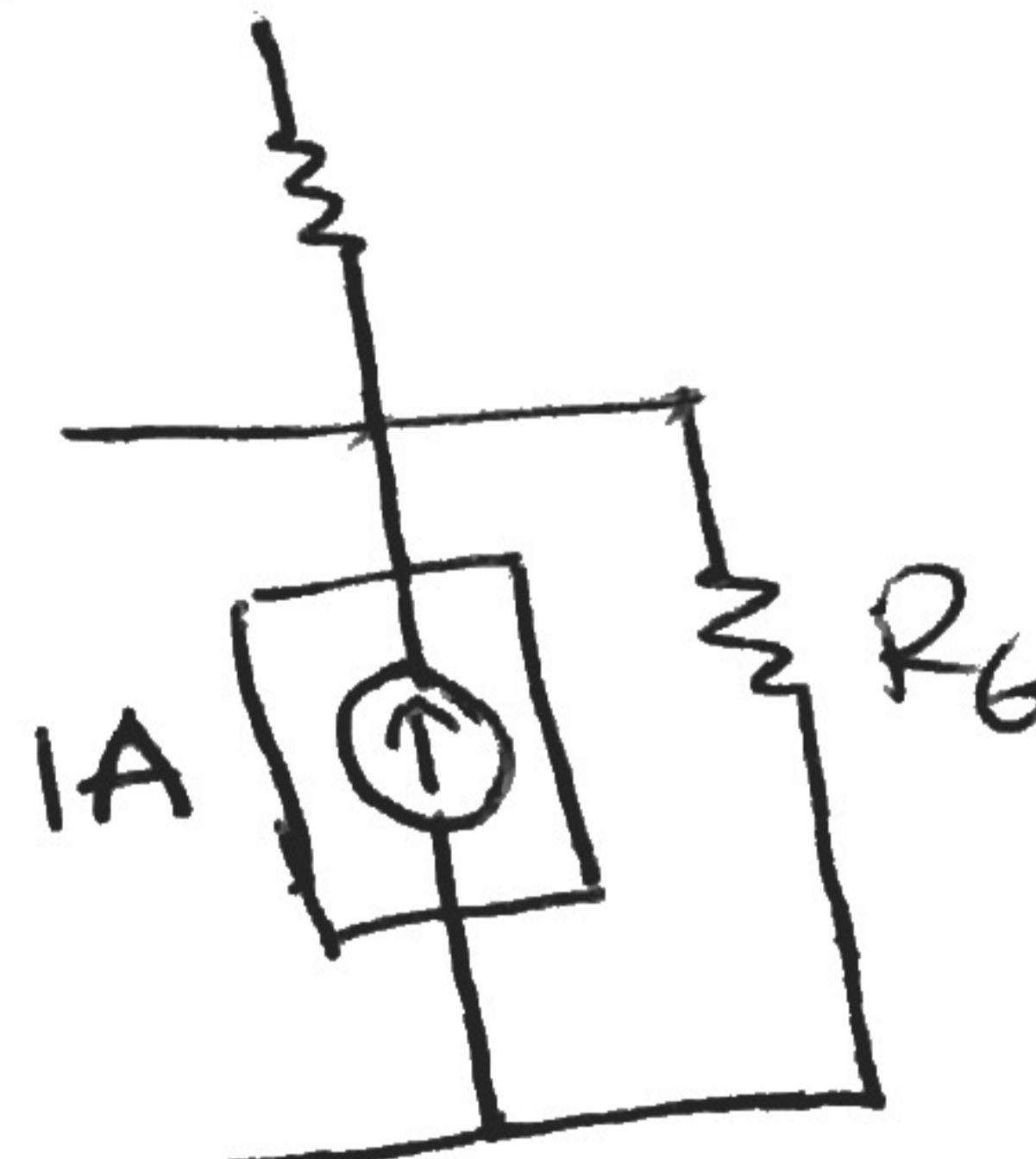
which is not consistent.

So, element inside the box can not be a VCVS.

\* Can it be an independent current source?

- YES!

No, problem with this.

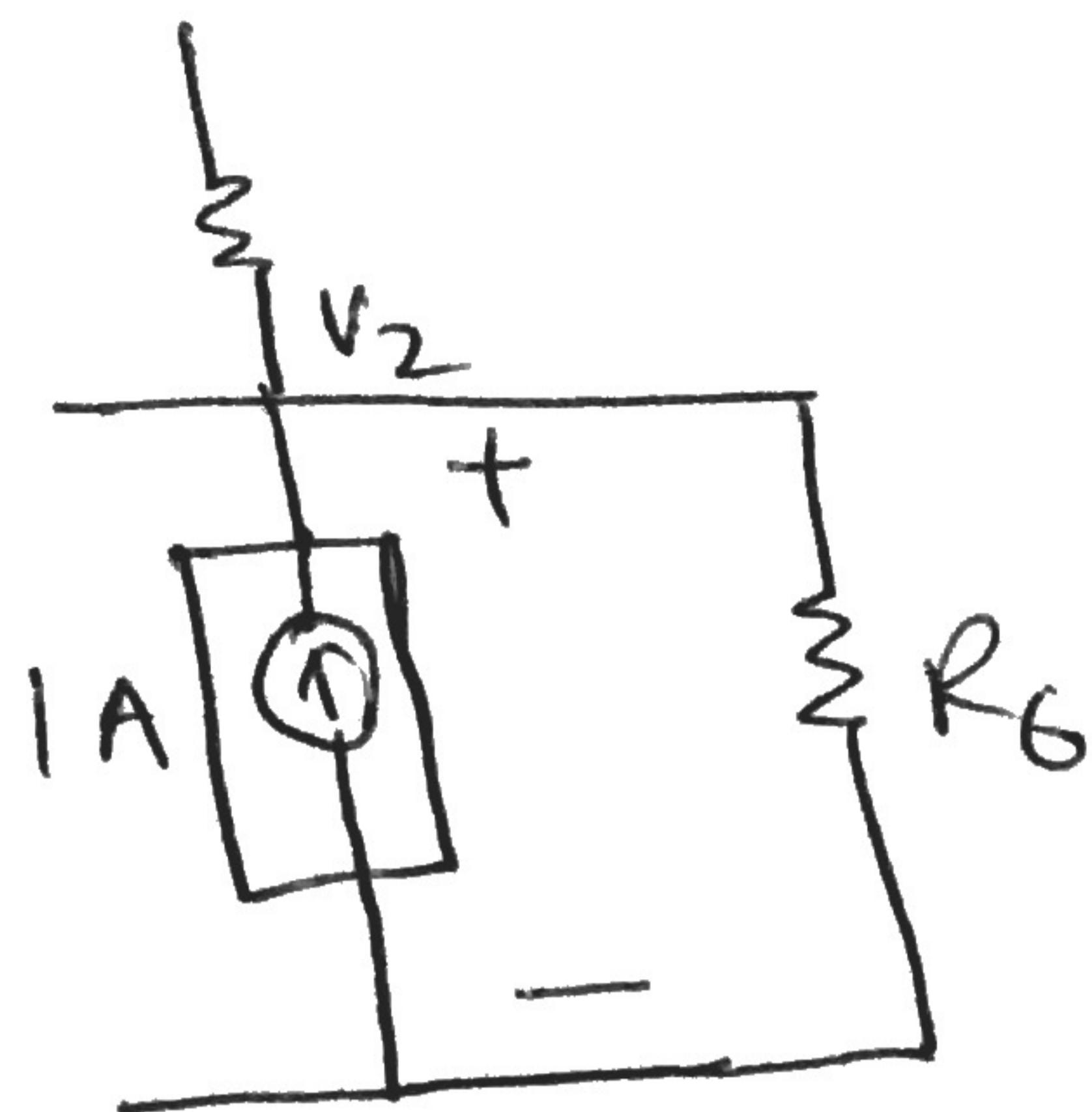


Can it be a dependent current source?

- NO. | The current in the branch consisting of the box has a constant value which does not vary with any other current or voltage.

Problem 1(b)

From part (a)



$V_2$  is positive. Now, According to passive sign convention,

$$\begin{aligned}\text{Power, } P &= V_2 \cdot i \\ &= 5 \times -1 \\ &= -5 \text{ W}\end{aligned}$$

$P < 0$ , so power is producing.  
Alternatively, positive current is flowing from negative to positive potential.  
So, power is producing.

## Rubrics for Problems 1 (a), (b)

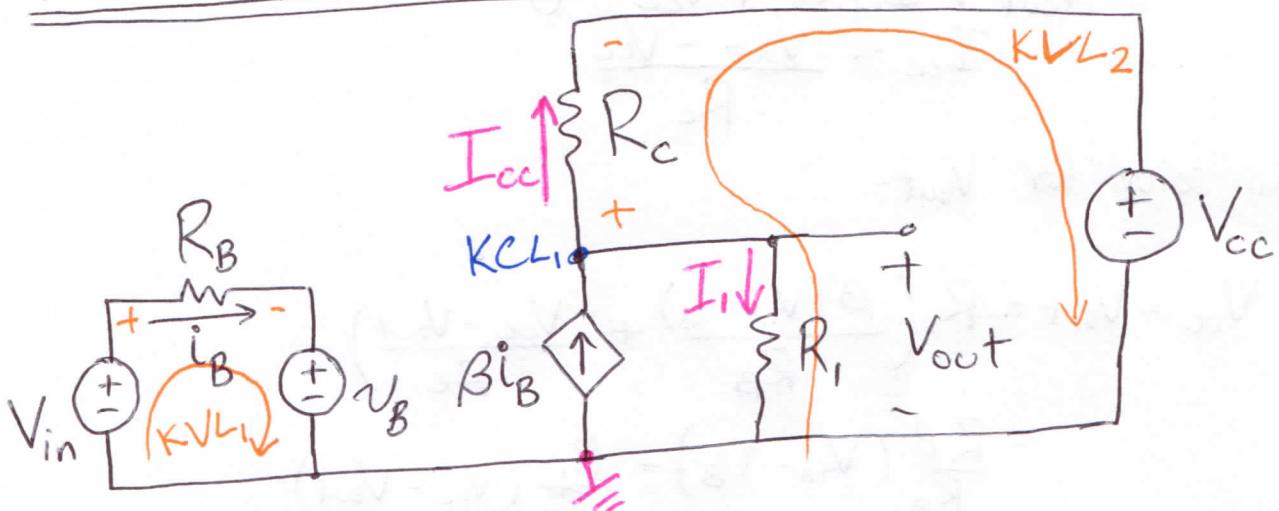
Problem 1 (a) - Total points: 10, negative scoring system used

Mistake	Penalty
Wrong value of the element in the box	4
Wrong circuit analysis (wrong current through the box element) and wrong element in the box	7
Right current through the box element but wrong element in the box	3
Right current through the box element but wrong or no symbol of the element in the box	1
Wrong polarity (arrow direction)/value combination of the current source in the box	1
No Work or Nothing is right	10

Problem 1 (b) - Total points: 5, negative scoring system used

Mistake	Penalty
If you did part a correct then this answer would be 'producing'. But blindly giving answer will not give you any point. We are judging your concept of power 'consuming' and 'producing' based on the current and voltage polarity of the element in the box that you found on part a. $P=VI$ . $P>0$ is Consuming, $P<0$ is Producing. V and I polarity should be consistent.	3
Incorrect answer	5

# PROBLEM 1 (c):



How to approach this problem:

The question asks for  $V_{TH}$  when seen across the  $V_{out}$  terminals. This means  $V_{oc} = V_{out} = V_{TH}$ . = voltage across  $R_i$ . To get this voltage, we need to find the current through  $R_i$ . There are two sources that contribute to this current:  $V_{cc}$  and  $\beta i_B$ .

So the first step would be to find  $i_B$ , then use the circuit techniques we learned in class (KVL, KCL, mesh, nodal,  $V=IR$ , etc..) to find  $V_{oc}$ .

Solution

**KVL**, around left loop to find  $i_B$ .

$$-V_{in} + R_B i_B + V_B = 0$$

$$i_B = \frac{V_{in} - V_B}{R_B}$$

**KCL** - for convenience, **gnd** is chosen at the bottom node.

$$\beta i_B = I_{cc} + I_i = I_{cc} + \frac{V_{out}}{R_i}$$

Solve for  $V_{out}$ :

$$\begin{aligned} V_{out} &= R_i (\beta i_B - I_{cc}) \\ &= R_i \left( \beta \left( \frac{V_{in} - V_B}{R_B} \right) - I_{cc} \right) \end{aligned}$$

KVL<sub>2</sub> around right loop to get an expression for  $I_{cc}$ .

$$-V_{out} + I_{cc}R_c + V_{cc} = 0$$

$$I_{cc} = \frac{V_{out} - V_{cc}}{R_c}$$

Now solve for  $V_{out}$ :

$$\begin{aligned} V_{oc} &= V_{out} = R_i \left( \frac{\beta(V_{in} - V_B)}{R_B} + \frac{V_{cc} - V_{out}}{R_c} \right) \\ &= \frac{R_i \beta}{R_B} (V_{in} - V_B) + \frac{R_i V_{cc}}{R_c} - \frac{R_i V_{out}}{R_c} \end{aligned}$$

$$\therefore V_{out} \left( 1 + \frac{R_i}{R_c} \right) = \frac{R_i \beta}{R_B} (V_{in} - V_B) + \frac{R_i V_{cc}}{R_c}$$

$$\Rightarrow V_{out} = V_{oc} = \left( \frac{R_c R_i}{R_c + R_i} \right) \left[ \frac{\beta}{R_B} (V_{in} - V_B) + \frac{V_{cc}}{R_c} \right]$$

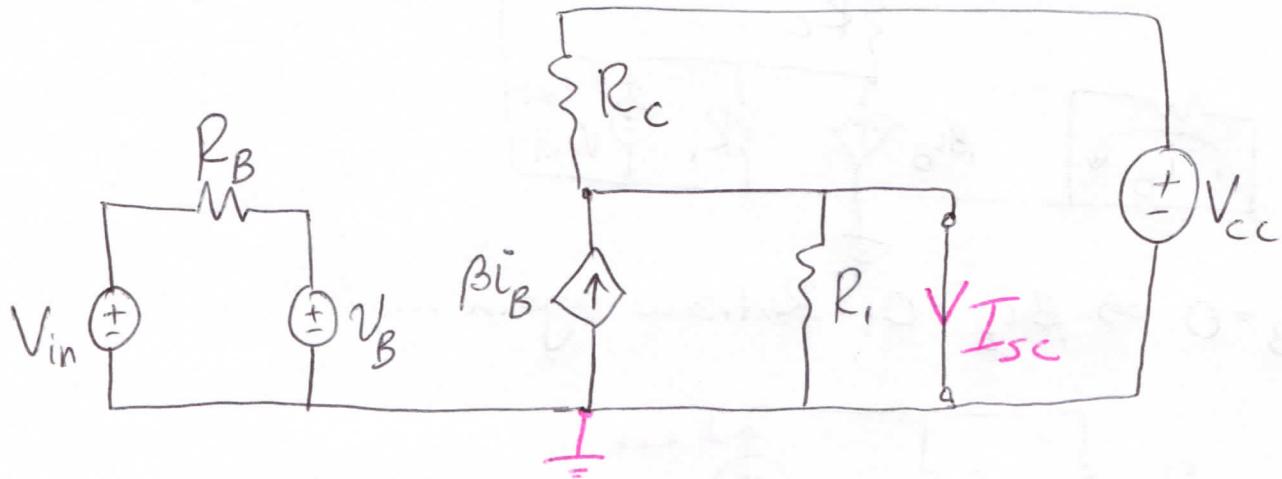
### PROBLEM 1(d) :

How to approach this problem:

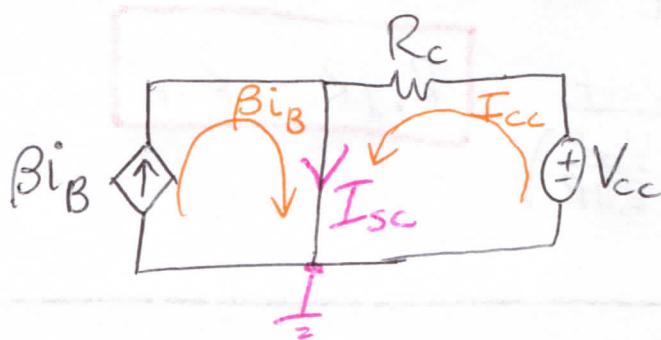
There are a couple of ways to find  $R_{TH}$ .

- ① We can find  $I_{sc}$  and the  $R_{TH}$  will equal  $V_{oc}/I_{sc}$ , OR
- ② apply an external test voltage (while turning off INDEPENDENT sources), measure the resulting current  $I_{ex}$ , and  $R_{TH}$  will equal  $V_{ex}/I_{ex}$ .

Method ① - Redraw the circuit shorting  $V_{out}$ .



$R_L$  is shorted out, so no current goes through it.  
Redrawing again, we get:

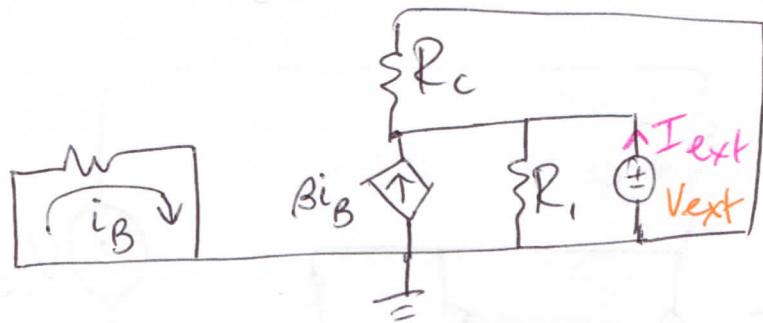


$$I_{sc} = \beta i_B + I_{cc} = \beta i_B + \frac{V_{cc}}{R_C}$$

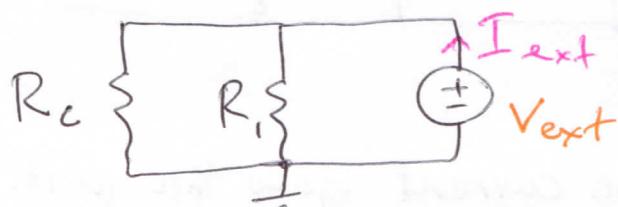
$$\text{AND, } i_B = \frac{V_{in} - V_B}{R_B}$$

$$R_{TH} = \frac{V_{oc}}{I_{sc}} = \left( \frac{R_C R_I}{R_C + R_I} \right) \frac{\beta i_B + V_{cc}/R_C}{\beta i_B + V_{cc}/R_C} \Rightarrow R_{TH} = \frac{R_C R_I}{R_C + R_I} = R_I // R_C$$

Method ② - Redraw circuit while turning off INDEPENDENT sources.



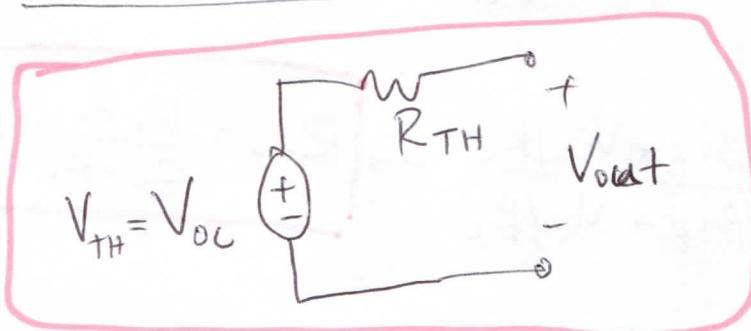
$i_B = 0 \Rightarrow \beta i_B = 0$ , Redraw again ...



$$I_{ext} = \frac{V_{ext}}{R_L \parallel R_c} \quad \left. \begin{array}{l} \text{Combined resistors and} \\ \text{used } V=IR \text{ here} \end{array} \right\}$$

$$\Rightarrow R_{TH} = \frac{V_{ext}}{I_{ext}} = \frac{V_{ext}}{\left( \frac{V_{ext}}{R_L \parallel R_c} \right)} = R_L \parallel R_c = R_{TH}$$

### PROBLEM 1 (e) :



PROBLEMS 1 c-e

Solutions by Divya Kashyap



# Rubrics for Problems 1 (c), (d), (e)

## Problem 1 (c) - Total points: 5, negative scoring system used

Mistake	Penalty
Didn't have KVL to find expression for $i_B$	1
Didn't have correct expression for $i_B$	1
Flaws in the method used for getting $V_{oc}$	2
Incorrect answer for $V_{out}$	1
Arithmetic error	0.5

## Problem 1 (d) - Total points: 5, negative scoring system used

Mistake	Penalty
Wrong answer, didn't show work, or not clear how student got the answer	5
Fundamental mistake: Wrong circuit, didn't calculate $I_{sc}$ , or didn't know $V = IR$	5
Shorted the dependent source	2.5
Correct circuit, but calculated $I_{sc}$ and/or $R_{th}$ wrong	2.5
Didn't calculate $I_{sc}$ correctly (wrong circuit or correct circuit, but wrong KVL/KCL, etc.,), but demonstrated that they know $R_{th} = V_{oc}/I_{sc}$ , or using a test source, $R_{th} = V_{ext}/I_{ext}$	4
Calculated $I_{sc}$ correctly, but had wrong $V_{th}$ in part (c) so got wrong $R_{th}$	1
Arithmetic error	0.5

**Problem 1 (e) – Total points: 5, negative scoring system used.** Here, if you got the wrong answers to  $V_{th}$  and  $R_{th}$ , you were already penalized in parts (c) and (d), so I just looked to see if you had placed the circuit elements and labeled them correctly.

Mistake	Penalty
Wrong circuit, or blank	5
Correct circuit, but didn't label $V_{th}$ (or labeled with a value that didn't match answer for part (c)), or made it a current source	2.5
Correct circuit, but didn't label $R_{th}$ (or labeled with a value that didn't match answer for part (d)), or placed it on the other side	2.5
Arithmetic error	0.5

Problem 2

- 1)  $V_1 = 10$
- 2)  $V_1 - V_2 = -20$
- 3) Form node 3:

$$\frac{V_2 - V_3}{R_7} = \frac{V_3 - V_1}{R_3} + \frac{V_3}{R_8} + \frac{V_3 - V_5}{R_9}$$

$$V_1 + V_2 - 4V_3 + V_5 = 0$$

- 4) Form node 4:

$$\frac{V_2 - V_4}{R_5} = \frac{V_4}{R_4} + \frac{V_4 - V_5}{R_6}$$

$$V_2 - 3V_4 + V_5 = 0$$

- 5) Form node 2 & 5:

$$\frac{V_4 - V_2}{R_5} + \frac{V_3 - V_2}{R_7} = i_x = \frac{V_5 - V_4}{R_6} + \frac{V_5 - V_3}{R_9}$$

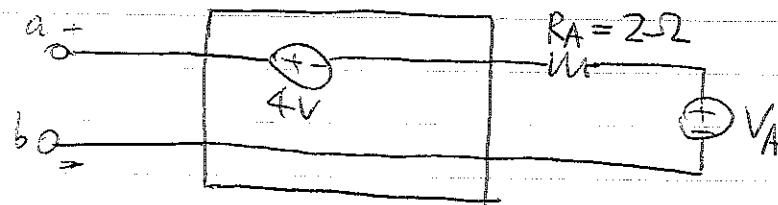
$$V_2 - V_3 - V_4 + V_5 = 0$$

\*each equation for 5 points

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Problem 3

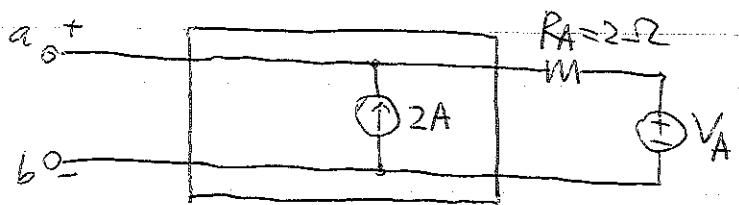
Sol:



$$R_A = 2\Omega$$

~~Need to say 4V &  $R_A = 2\Omega$  to get full points.~~

OR



$$R_A = 2\Omega$$

~~Need to say 2A &  $R_A = 2\Omega$  to get full points.~~

OR, if you put more than 1 element into the box, you will receive ~~no~~ full points as long as your solution fulfills all three requirements as follows:

- (a) The open circuit voltage across terminals a,b is 5V.
- (b) The short circuit current from terminal a to b is 2.5 A
- (c) A correct value of  $R_A$  that goes with your ~~circuit~~ circuit.

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Problem 4.

Mesh 1:  $I_1 R_2 + R_3 (I_1 - I_2) + R_4 (I_1 - I_3) + R_1 I_1 = 0 \quad (a) \quad (5 \text{ pts})$

OR

$$I_1 + I_4 - I_1 + 10(I_1 - I_3) + 10I_1 = 0$$

From Loop 2:  $I_2 = I_A = 1 \quad (b) \quad (4 \text{ pts})$

Supernode 3 & 4:  $V_0 = R_4 (I_3 - I_1) + V_1 + R_6 I_4 \quad (c) \quad (5 \text{ pts})$

OR

$$0.5 = 10(I_3 - I_1) + 0.5 + 10I_4$$

$I_4 - I_3 = I_B = 1 \quad (d) \quad (5 \text{ pts})$

$$I_1 = -\frac{4}{17} \quad (1 \text{ pts})$$

$$I_5 = 0 \quad (5 \text{ pts})$$

If you list 5 equations, including  $I_5$ , and those equations are correct / similar to equ (a)-(d), you will get points accordingly. Also, if your 5 equations are correct but your solved  $I_5 \neq 0$ , for (b), you will get 4 pts.

For example:

$$\textcircled{1} \quad R_1(I_1 - I_5) + R_2(I_4 - I_5) + R_3(I_4 - I_2) + R_4(I_4 - I_3) = 0$$

$$\textcircled{2} \quad -V_1 + R_3(I_2 - I_1) + R_2(I_5 - I_4) + R_1(I_5 - I_1) + V_0 \\ + I_5(R_7 + R_8 + R_9 + R_{10} + R_{11} + R_{12} + R_{13} + R_{14}) + R_6(I_5 - I_4) = 0$$

$$\textcircled{3} \quad I_2 - I_5 = I_A$$

$$\textcircled{4} \quad -V_0 + R_4(I_3 - I_4) + V_1 + R_6(I_4 - I_5) = 0$$

$$\textcircled{5} \quad I_4 - I_3 = I_B$$

$$\Rightarrow \left[ \begin{array}{ccccc} 22 & -1 & -10 & 0 & -11 \\ -12 & 1 & 0 & -10 & 29 \\ 0 & 1 & 0 & 0 & -1 \\ -1 & 0 & 1 & 1 & -1 \\ 0 & 0 & -1 & 1 & 0 \end{array} \right] \cdot \left[ \begin{array}{c} I_1 \\ I_2 \\ I_3 \\ I_4 \\ I_5 \end{array} \right] = \left[ \begin{array}{c} 0 \\ 0 \\ 1 \\ 0 \\ 1 \end{array} \right]$$

If you give above equation equations  $\textcircled{1} - \textcircled{5}$  OR give the above matrix correctly, you will get 19 points for part(a) & 4 points for part (b) without numerically solved  $I_1$  &  $I_5$ .

\* A quicker way to solve for  $I_5$

