## EE 120 SIGNALS AND SYSTEMS, Fall 2012

Midterm \# 2, November 5, Monday, 10:10-11:50 am
Name $\qquad$
Closed book. Two letter-size cheatsheets are allowed. Show all your work. Credit will be given for partial answers.

| Problem | Points | Score |
| :---: | :---: | :---: |
| 1 | 20 |  |
| 2 | 20 |  |
| 3 | 20 |  |
| 4 | 20 |  |
| 5 | 20 |  |
| Total | 100 |  |

1. Given the frequency response:

$$
H(j \omega)=10 \frac{1-j \omega}{1+j \omega}
$$

a) (5 points) Sketch the Bode plot, labeling the relevant frequencies, and magnitude and phase values.
b) (5 points) Give an exact expression for the phase delay.
c) (5 points) Give an exact expression for the group delay.
d) (5 points) Determine the response of the system to the input $x(t)=\cos (t)$.

Additional workspace for Problem 1
2. A continuous time signal $x(t)$ with the spectrum $X(j \omega)$ depicted below is impulsetrain sampled with period $T_{1}$. One period of the resulting spectrum $X_{p}(j \omega)$ is shown below.

a) (10 points) Determine the largest sampling period $T_{2}$ that would avoid aliasing, and express it in terms of $T_{1}$.
b) (10 points) Sketch the spectrum $X_{p}(j \omega)$ for each of the following two sampling periods: (i) $T=T_{2}$, (ii) $T=2 T_{2}$.

Additional workspace for Problem 2
3. The continuous-time signal:

$$
x(t)=\cos \left(\omega_{0} t\right)
$$

is sampled with frequency $\omega_{s}=\frac{3 \omega_{0}}{2}$.
a) (5 points) Determine the resulting discrete-time signal $x[n]$.
b) ( 8 points) Suppose $x[n]$ is upsampled with $N=2$ (that is, expanded in time by a factor of $N=2$ and the missing samples are obtained from the existing ones with bandlimited interpolation). What is the resulting signal $x_{u}[n]$ ?
c) (7 points) Suppose now $x(t)$ is sampled with frequency $2 \omega_{s}$. Do the samples match $x_{u}[n]$ in part (b)? For which values of $\omega_{s}$ would sampling followed by upsampling with $N$ generate the same result as sampling with rate $N \omega_{s}$ ?

Additional workspace for Problem 3.
4. a) (15 points) Find the right-sided signal $x(t)$ whose Laplace transform is:

$$
X(s)=e^{-s} \frac{(s+1)^{2}}{s^{2}-s+1}
$$

b) (5 points) Find the unilateral Laplace transform for $x(t)$ in part (a).

Additional workspace for Problem 4.
5. A LTI system has a rational transfer function with the pole/zero pattern below:

a) (10 points) Indicate all possible regions of convergence (ROC) that can be associated with this pattern.
b) (10 points) For each ROC identified in part (a), determine whether the system is stable and/or causal.

Additional workspace for Problem 5.

