

EECS 40, Spring 2007
Prof. Chang-Hasnain
Midterm #1

September 17, 2007
 Total Time Allotted: 50 minutes
 Total Points: 100

1. This is a closed book exam. However, you are allowed to bring one page (8.5" x 11"), single-sided notes.
2. No electronic devices, i.e. calculators, cell phones, computers, etc.
3. **SHOW** all the steps on the exam. Answers without steps will be given only a small percentage of credits. Partial credits will be given if you have proper steps but no final answers.
4. Draw **BOXES** around your final answers.
5. **Remember to put down units.** Points will be taken off for answers without units.

Last (Family) Name: _____

First Name: _____

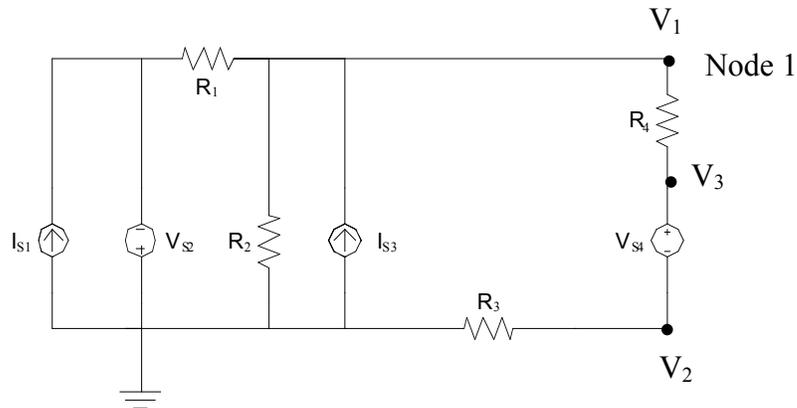
Student ID: _____ Discussion Session: _____

Signature: _____

Score:	
Problem 1 (25 pts)	
Problem 2 (43 pts):	
Problem 3 (32 pts)	
Total	

1. (25 pts) Node-Voltage Analysis

All voltages of the voltage sources, the currents of the current sources and the values of the resistors are given.



- a) (7 pts) Does the current source I_{S1} have impact on voltages V_1 and V_2 ? Justify your answer. (Hint: You do not need to solve the rest of the problem to do this part!!)

I_{S1} does not impact V_1 and V_2 since it is in parallel with V_{S3} and thus has the same voltage as V_{S3} . Also if one sets I_{S1} to 0 then it is clearly seen that it has no effect.

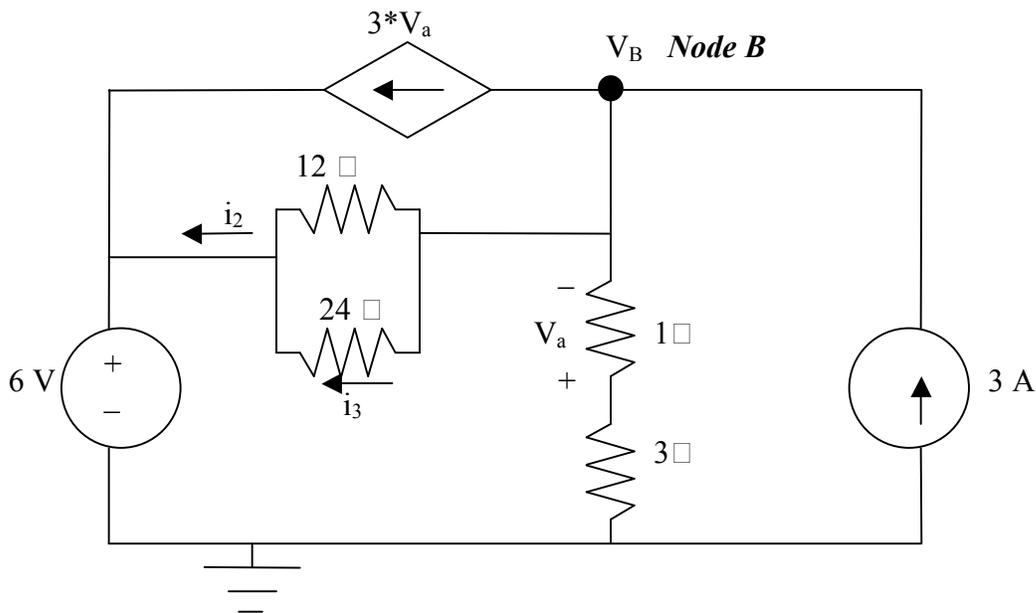
- b) (12 pts) Write KCL equation for node 1.

$$I_{S3} - (V_1 - V_{S2})/R_1 - V_1/R_2 - (V_1 - V_3)/R_4 = 0$$

- c) (6 pts) Consider the two terminals surrounding V_{S4} a super node. Write a KCL equation for the branch connecting R_4 , R_3 and V_{S4} .

$$-(V_3 - V_1)/R_4 - V_2/R_3 = 0$$

2. (43 pts) Dependent Source



a) (4 points) Write V_a in terms of V_B (the voltage at node B).
 $V_a = -1/4 V_B$ (by Voltage Divider Equation)

b) (18 points) Use KCL at node B, and your answer to part (a), to write an expression for V_B in terms of i_2 and constants in the problem.

$$3 - V_B/4 - 3 \cdot V_a - i_2 = 0$$

$$3 - V_B/4 + 3/4 \cdot V_B - i_2 = 0$$

$$V_B = 2(i_2) - 6$$

c) (8 points) Use KVL and Ohm's Law (of parallel resistors) to write an expression for i_2 in terms of V_B and constants in the problem.

$$V_B - 6 = 8 \cdot i_2$$

$$V_B = 8(i_2) + 6$$

- d) (8 points) Solve for V_B and i_2 . Hint: both should be integers. If they are not, go back and check your work.

Combining b and c

$$2(i_2) - 6 = 8(i_2) + 6$$

$$6(i_2) = -12$$

$$i_2 = -2 \text{ A}$$

Plugging this back into c) you get:

$$v_b = -10 \text{ V}$$

- e) (5 points) Determine the value of i_3 .

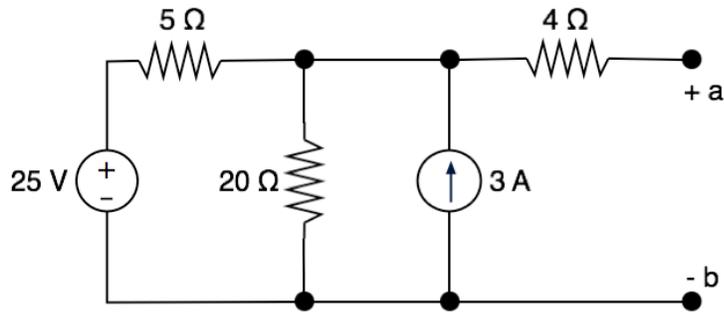
Using Current Divider equation:

$$i_3 = (i_2) \left(\frac{12}{12+24} \right)$$

$$i_3 = -2/3 \text{ A}$$

3. (32 pts) Thévenin and Norton Equivalent Circuits

- (a) (18 pts) Looking into terminals across a and b. What are the open circuit voltage V_{ab} , and the Thévenin Resistance R_{th} ?



Let $V_b=0$, $V_{ab}=V_a$

$$(25-V_a)/5+3=V_a/20$$

$$8=V_a (1/5+1/20)=V_a (1/4)$$

$$V_a=V_{ab}=32 \text{ V}$$

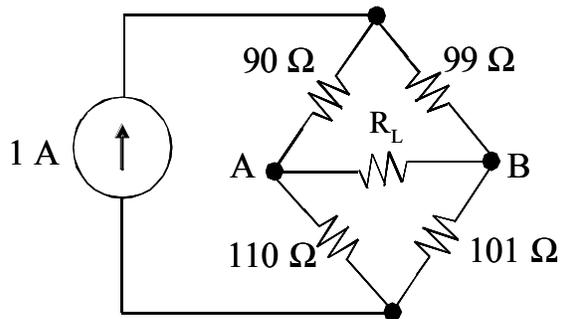
Thevenin Resistance

Voltage source is short, current source is open.

$$5 \Omega \text{ parallel with } 20 \Omega = 4 \text{ Ohm}$$

$$4 \text{ Ohm in series with } 4 \text{ Ohm} = R_{th}=8 \text{ ohms}$$

(b) (7 pts) Looking into terminals across A and B. What is the open circuit voltage V_{ab} ?



Current in each path is equal at 0.5 A.
 $V_{ab} = 0.5 (110 - 101) = 4.5V$

(c) (7 pts) Same circuit as above, looking into terminals across A and B. What is the Thevenin Resistance R_{th} ? (You do not need to carry out the division.)

Thevenin Resistance
Current source is open.

$(99 + 90) // (101 + 110) = 211 * 189 / 400 \text{ Ohm}$