# EECS 105, Fall 1993 <br> Midterm \#2 <br> Professor R. T. Howe 

## Ground Rules:

- Closed book and notes; one formula sheet (both sides)
- Do all work on exam pages
- Answers accurate to within $10 \%$ will receive full credit
- Default bipolar transistoe parameters:
$n p n:(\text { beta })_{n}=100, V_{A n}=50 \mathrm{~V}, I_{S n}=10-16 \mathrm{~A}$.
pnp: $(\text { beta })_{p}=50, V_{A p}=25 \mathrm{~V}, I_{S p}=10^{-16} \mathrm{~A}$.
- Default MOS transistor parameters:

NMOS: $(m u)_{n} C_{o x}=50(\mathrm{mu}) \mathrm{AV}^{-2},(\text { lambda })_{n}=0.02 \mathrm{~V}^{-1}, V_{T n}=1 \mathrm{~V}$.
PMOS: $(m u)_{p} C_{o x}=25(\mathrm{mu}) \mathrm{AV}^{-2},\left(\right.$ lambda $_{p}=0.02 \mathrm{~V}^{-1}, V_{T p}=-1 \mathrm{~V}$.

## Problem \#1. Matched Complementary Bipolar Transistor Design [12 points]

The cross sections, minority carrier concentrations, and circuit schematics are shown for matched npn and pnp vertical BJTs, operated in the forward-active region.


Given: all doping levels are matched and the emitter areas are identical

- $N_{d E}(\mathrm{npn})=N_{a E}(\mathrm{pnp})$
- $N_{a B}(\mathrm{npn})=N_{d B}(\mathrm{pnp})$
- $N_{d C}(\mathrm{npn})=N_{a C}(\mathrm{pnp})$
- $A_{E}(\mathrm{npn})=A_{E}(\mathrm{pnp})$

Given: the bias volatages for the two transistors are matched and both are in the forward-active region

- $V_{B E n}=V_{E B p}$
- $V_{C E n}=V_{E C p}$
(a) [5 pts.] In order for the npn and the pnp transistors to have matched collector currents, $I_{C n}=\left|I_{C p}\right|$, determine the numerical value of the base width of the pnp, $W_{B p}$. Given: the base width of the npn is $W_{B n}=0.2(\mathrm{mu}) \mathrm{m}$, the electron diffusion coefficient (diffusivity) is $D_{n}=20 \mathrm{~cm}^{2} \mathrm{~s}^{-1}$, and the hole diffusivity is $D_{p}=10 \mathrm{~cm}^{2} \mathrm{~s}^{-1}-$ these are valid for the emitter, base, and collector of each transistor.
(b) [5 pts.] In order for the npn and the pnp transistors to matched base currents, $I_{B b n}=\left|I_{B p}\right|$, determine the numerical value of the emitter width of the pnp, $W_{E p}$. This part is independent of part (a). Given: the emitter width of the npn is $W_{E n}=0.1(\mathrm{mu}) \mathrm{m}$, and $D_{n}=20 \mathrm{~cm}^{2} \mathrm{~s}^{-1}, D_{p}=10 \mathrm{~cm}^{2} \mathrm{~s}^{-1}$.
(c) [2 pts.] Which transistor has the smaller Early voltage, $V_{A}$ ? Explain why in one sentence.


## Problem \#2. Two-Stage Transconductance Amplifier [24 points]



Given: $I_{\text {REF }}=100(\mathrm{mu}) \mathrm{A}, V_{L}=0(\mathrm{DC}), R_{S}=1 \mathrm{k}($ omega $), R_{L}=400 \mathrm{k}($ omega $)$
MOSEFTs: $(W / L)_{3,5,6,7}=10$ and $(W / L)_{4}=25$
(a) [4 pts.] Find the collector currents $I_{C I}$ and $I_{C 2}$. You can neglect the base currents $I_{B I}$ and $I_{B 2}$, as is customary for hand calculations.
(b) $\left[4\right.$ pts.] Find the numerical value of the input resistance, $R_{i}$ of this amplifier. If you couldn't answer part (a), you can assume that $I_{C 1}=50(\mathrm{mu}) \mathrm{A}$ and that $I_{C 2}=75(\mathrm{mu})$ A for this part.
(c) $\left[4\right.$ pts.] Find the numerical answer value of the output resistance, $R_{o}$ of this amplifier. If you couldn't answer part (a), you can assume that $I_{C 1}=50(\mathrm{mu}) \mathrm{A}$ and that $I_{C 2}=75(\mathrm{mu})$ A for this part.
(d) [4 pts.] Find the numerical value of the short-circuit transconductance $G_{m}$ of the amplifier. Again, if you couldn't answer part (a), you can assume that $I_{C 1}=50(\mathrm{mu}) \mathrm{A}$ and that $I_{C 2}=75(\mathrm{mu}) \mathrm{A}$ for this part.
(e) [5 pts.] Find the numerical value of the laod current $i_{l}$, for a small-signal input voltage $v_{s}=2 \mathrm{mV}$. If you couldn't solve parts (b), (c), and (d), asumme for this part that $R_{i}=80 \mathrm{k}$ (omega), $R_{o}=500 \mathrm{k}$ (omega), and $G_{m}=7.5 \mathrm{mS}$.
(f) [3 pts.] What is the DC voltage at the base $Q_{I}$ ? You can assume that $V_{B E}=0.7 \mathrm{~V}$ for the transistors in the forward-active region.

## Problem \#3. Current-Source Design [14 points]



Given: $(W / L)_{1}=(W / L)_{2}=(W / L)_{3}$
(a) [5 pts.] Find $(W / L)_{1}$ such that $I_{R E F}=20(\mathrm{mu}) \mathrm{A}$.
(b) $\left[3 \mathrm{pts}\right.$.] Find $(W / L)_{4}$ such that $I_{O U T}=50(\mathrm{mu})$ A. If you couldn't solve part $(\mathrm{a})$, assume that $(W / L)_{1}=$ 10.
(c) $\left[3\right.$ pts.] Find the numerical value of $r_{o c}$ for this current source, assuming that $I_{O U T}=50(\mathrm{mu}) \mathrm{A}$.
(d) [3 pts.] Assuming that the source-gate voltage for transistor $M_{4}$ is $V_{S G 4}=1.4 \mathrm{~V}$. What is the largest DC output voltage $V_{O U T}$ for which transistor $M_{4}$ remains in the saturation region?

## Posted by HKN (Electrical Engineering and Computer Science Honor Society) University of California at Berkeley <br> If you have any questions about these online exams please contact mailto:examfile@hkn.eecs.berkeley.edu

