## Final: Total 200 points (3-hour exam)

## [Engineering Economics]

## IRR Calculation [15 points]

One alternative for improving a company's operations is to do nothing for the next 2 years and then spend $\$ 10,000$ on operations. If this course of action is followed, the following cash flow will result:

| End of Year | Cash Flow |
| :---: | :---: |
| 0 | $+\$ 3000$ |
| 1 | $\$ 0$ |
| 2 | $-\$ 10,000$ |
| 3 | $+\$ 2000$ |
| 4 | $+\$ 2000$ |
| 5 | $+\$ 2000$ |
| 6 | $+\$ 2000$ |

What rate of return can be expected from this cash flow? And under what condition would this proposal be attractive?

## Solution:

| IRR | Net Present Worth |
| :---: | :---: |
| $0 \%$ | $+\$ 1000$ |
| $9.4 \%$ | $\$ 0$ |
| $10 \%$ | $-\$ 25$ |
| $20 \%$ | $-\$ 350$ |
| $30 \%$ | $-\$ 353$ |
| $40 \%$ | $-\$ 215$ |
| $50 \%$ | $-\$ 2$ |
| $51 \%$ | $\$ 0$ |

According to the results of mathematical calculation, the proposal is attractive when the external rate of return is below $9.4 \%$ or above $51 \%$. However, $51 \%$ of interest rate is not realistic. This means that IRR method has flaw of having more than one rate in some cases and this flaw should be considered in making decisions.

## [Project Evaluation and Selection]

## Challenger-Defender Method (Incremental Method) [20points]

You have three alternative plans of operation for the next 6 years. All transactions occur in the beginning of the year. (Interest Tables and Formulas are attached at the end.)

1) Plan A: Do nothing for first 2 years and invest $\$ 10,000$ in the third year. This will yield an annuity of $\$ 3,200$ starting in the 4th year until the 7th year.
2) Plan B: Do nothing this year and invest $\$ 7,000$ next year. The annuity will be $\$ 1,800$ from the 3rd year to the 7th year.
3) Plan C: Invest $\$ 8,000$ now and earn an annuity of $\$ 1,200$ starting in the 2nd year.

The minimum attractive rate of return is $8 \%$. Which plan would you choose?

## Answers:

| Year | Transaction Point on | Cash Flow |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Cash Flow Diagram | Plan A | Plan B | Plan C |
| 1st | 0 | 0 | 0 | $-8,000$ |
| 2nd | 1 | 0 | $-7,000$ | $+1,200$ |
| 3rd | 2 | $-10,000$ | $+1,800$ | $+1,200$ |
| 4th | 3 | $+3,200$ | $+1,800$ | $+1,200$ |
| 5th | 4 | $+3,200$ | $+1,800$ | $+1,200$ |
| 6th | 5 | $+3,200$ | $+1,800$ | $+1,200$ |
| 7th | 6 | $+3,200$ | $+1,800$ | $+1,200$ |

## Step 1:

$$
\begin{aligned}
\text { PV }(\text { Plan } A) & =-10,000(P / F, 8 \%, 2)+3,200(P / A, 8 \%, 4)(P / F, 8 \%, 2) \\
& =-10,000 * 0.8573+3,200 * 3.3121^{*} 0.8573=\$ 513 \rightarrow \text { OK } \\
\text { PV (Plan B) } & =-7,000(P / F, 8 \%, 1)+1,800(P / A, 8 \%, 5)(P / F, 8 \%, 1) \\
& =-7,000 * 0.9259+1,800 * 3.9927^{*} 0.9259=\$ 173 \rightarrow \text { OK } \\
\text { PV (Plan C) } & =-8,000+1,200(P / A, 8 \%, 6)=-8,000+1,200 * 4.6229=-\$ 2452 \rightarrow \text { Reject! }
\end{aligned}
$$

## Step 2:

Compare the amount of investment (ignore the different timing of investment): $\mathrm{B}<\mathrm{A}$

| Year | Transaction Point on | Cash Flow |
| :---: | :---: | :---: |
|  | Cash Flow Diagram | $\mathbf{B} \rightarrow \mathbf{A}(\mathbf{A}-\mathbf{B})$ |
| 1st | 0 | 0 |
| 2nd | 1 | $+7,000$ |
| 3rd | 2 | $-11,800$ |
| 4th | 3 | $+1,400$ |
| 5th | 4 | $+1,400$ |
| 6th | 5 | $+1,400$ |
| 7th | 6 | $+1,400$ |
| PV |  |  |
|  | Decision | $\mathbf{A}$ |

```
PV (B->A) = 7,000 (P/F, 8%, 1) - 11,800 (P/F, 8%, 2) + 1,400 (P/A, 8%, 4) (P/F, 8%, 2)
    = 7,000 * 0.9259-11,800 * 0.8573 + 1,400 * 3.3121 * 0.8573 = $340
Going from B to A is good, Choose A
```


## Final Choice is A

## Decision Tree [20 points]

A project manager is planning an activity that requires use of a crane. He has two alternatives; a medium size crane or a large size crane. The rent is $\$ 10,000$ for the medium sized one and $\$ 15,000$ for the large one. Because of its greater capacity, the large crane can accomplish the activity faster, therefore the probability of the work being delayed is lower.

| Type of Crane <br> to Choose | Rent | Probability of <br> being delayed |
| :---: | :---: | :---: |
| Medium | $\$ 10,000$ | 0.3 |
| Large | $\$ 15,000$ | 0.2 |

Once the work is delayed, no matter which crane is used, the probability that the delay becomes 'long delay' is $20 \%$. The probabilities that the delay becomes 'medium delay' and 'short delay' are $50 \%$ and $30 \%$, respectively. The costs of delay are different for the types of cranes. The costs of the delay will also vary depending on the types of the delay. This information is tabulated below.

| Crane Type | Type of Delay | Probability | Cost of Delay |
| :---: | :---: | :---: | :---: |
| Medium | Long Delay | 0.2 | $\$ 50,000$ |
|  | Medium Delay | 0.5 | $\$ 25,000$ |
|  | Short Delay | 0.3 | $\$ 10,000$ |
| Large | Long Delay | 0.2 | $\$ 15,000$ |
|  | Medium Delay | 0.5 | $\$ 10,000$ |
|  | Short Delay | 0.3 | $\$ 5,000$ |

(a) Which crane size should the project manager choose? Develop the decision tree and calculate the EV (Expected Value) for each crane. Please make it clear what are the decision nodes and chance nodes.
(b) Discuss your solution; which variable, when changed, is most likely to lead to the opposite result or decision? Limit your answer to 2-3 sentences.

## Decision Tree Diagram:



Calculation:

| EMV | Calculation | Choice |
| :---: | :---: | :---: |
| Chance Node 4 | -50 * $0.2-25$ * $0.5-10$ * $0.3=-25.5 \mathrm{~K}$ | $\begin{gathered} \text { Total Cost for Medium: } \\ \$ 17,650 \\ \text { Total Cost for Large: } \\ \$ 16,900 \\ \rightarrow \text { Choose Large Crane! } \end{gathered}$ |
| Chance Node 5 | -15 * 0.2-10 * $0.5-5$ * $0.3=-9.5 \mathrm{~K}$ |  |
| Chance Node 2 | -25.5 * $0.3+0$ * $0.7=-7.65 \mathrm{~K}$ |  |
| Chance Node 3 | -9.5 * $0.2+0$ * $0.8=-1.9 \mathrm{~K}$ |  |
| Decision Node 1 | Medium: -10K $-7.65 \mathrm{~K}=-17.65 \mathrm{~K}$ |  |
|  | Large: -15K-1.9K = - 16.9K |  |

## EV of Perfect Information [20 points]

You are planning to construct a vacation house on land you've recently purchased. You are expecting to make profits by renting the house.

Then you learned that there would be a 10 \% chance of a mudslide in that area within five years after construction. In case of a mudslide, you are responsible for fixing any damage to the property.

You have two choices to make; (1) you spend extra \$ to harden the ground around the house and reduce the damage in case of a mudslide or (2) just ignore the chance of a mudslide. The damage will be greater in the latter case.

The profits for the alternatives are tabulated below.

|  | Mudslide (0.1) | No mudslide (0.9) |
| :--- | :---: | :---: |
| (1) Extra ground work in addition to house | $\$ 40,000$ | $\$ 50,000$ |
| (2) No extra ground work, only house | $-\$ 20,000$ | $\$ 70,000$ |

(a) Which alternative would you choose?
(b) Suppose you can get perfect information about whether there will be a mudslide within five years, by going to a consultant. But there is a consulting fee of $\$ 5,000$. Would you pay the consultant to get the perfect information?

## Answers:

(a) Calculate EV's for each option and compare them.

$$
\begin{aligned}
& \text { EV(Alt.1) }=40,000 * 0.1+50,000 * 0.9=49,000 \\
& \text { EV(Alt.2) }=-20,000 * 0.1+70,000 * 0.9=61,000
\end{aligned}
$$

Choose the one that gives the bigger EV. $\rightarrow$ Alternative 2
(b) Calculate the EV when you have the perfect information. If you know there will be a mudslide for sure, you will choose the option (1). If you know there will be no mudslide for sure, you will choose the option (2).

EV (Perfect Info $)=40,000$ * $0.1+70,000$ * $0.9-5,000=67,000-5,000=62,000$
Compare this EV with the EV when you have no perfect information;
$E V($ No Info $)=61,000<E V($ Perfect $\operatorname{Info})=62,000 \rightarrow \underline{\text { Pay the consultant! }}$

## [Scheduling]

## CPM with Lead-Lag Relationships [15 points]

(a) For the following activities, draw AON and find the ES, EF, LS, LF, TF, and FF. Record your answers neatly in a table. Identify critical paths. [5 points]

| Activity | Predecessor | Duration |
| :---: | :---: | :---: |
| A | - | 3 |
| B | A | 5 |
| C | B | 10 |
| D | A | 4 |
| E | B, D | 5 |
| F | B, D | 7 |
| G | E, F | 6 |
| H | C, G | 2 |

(b) The contractor reviewed the schedule of (a) and added following lead-lag relationships: (1) Activity E still follows B and D but needs to wait 2 days after $D$ finishes to be able to begin, (2) G can start as soon as 5 days after F's start allowing concurrency, and (3) C needs to be completed at least 3 days before H finishes.

Draw AON and find the ES, EF, LS, LF, TF, and FF and record them neatly in a table. Identify critical paths. Describe the differences specifically and concisely. What is the managerial implication of the changes resulting from the lead-lag relationships? [10 points]

## Answers:

(A) AON


CP: A-B-F-G-H


0 B 0
459
(b) AON


CP: A-D-E-G-H

| Activity | ES | EF | LS | LF | TF | FF |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | 1 | 4 | 1 | 4 | 0 | 0 |
| B | 4 | 9 | 5 | 10 | 1 | 0 |
| C | 4 | 8 | 4 | 8 | 0 | 0 |
| D | 9 | 19 | 10 | 20 | 1 | 1 |
| E | 10 | 15 | 10 | 15 | 0 | 0 |
| F | 9 | 16 | 10 | 17 | 1 | 1 |
| G | 15 | 21 | 15 | 21 | 0 | 0 |
| H | 21 | 23 | 21 | 23 | 0 | 0 |

## Discussion:

CP has changed from ABFGH to ADEGH. Total duration has reduced from 23 days (finishing date is 24 ) to 22 days (finishing date is 23). This reduction was mainly because the SS relationship between F and G allowed overlapping of 2 days although $\mathrm{FS}=2$ between D and E canceled out the possible full 2 day reduction. Now the new schedule has less flexibility; total floats of all paths have decreased. All paths are now near critical. C also became critical due to the FF relationship. More attention and care should be taken by management to stay on time.

## [Estimating the Durations of Activities]

## Learning Curve Effect [20 points]

A task is to be repeated 6 times in a project. Its duration is estimated to be 100 work-hours for the first time if performed by a single worker. The task has a $90 \%$ learning curve. Indicate the work-hours by one decimal number.
(a) What is the estimated duration of the task considering the effect of the learning curve?
(b) What if the task is done by two workers? What would be the estimate of their total duration?
(c) Now consider the single worker case. You've just acquired some information that the task might have to be stopped after the 3rd repetition of the work. The work can be resumed after 30 work-hours. However, because of this stoppage, the worker will lose job rhythm. Therefore when he comes back to the site and starts 4th repetition, he will only have the productivity equal to having finished the first repetition. Knowing this condition, what would be your estimate of duration for this task?
(d) How many hours can be accounted for by the loss of productivity due to stoppage of work in situation (c)?

## Formulas:

$$
\begin{gathered}
\beta=\log _{10} L / \log _{10} 2 \\
T_{N}=T_{1} \times N^{\beta}
\end{gathered}
$$

## Answers:

$\mathrm{L}=0.9$ and $\mathrm{T}_{1}=100$
$\beta=\log _{10} 0.9 / \log _{10} 2=\underline{\mathbf{0 . 1 5 2}}$
$\mathrm{T}_{\mathrm{N}}=\mathrm{T}_{1} \times \mathrm{N}^{-0.152}$

| $*$ <br> R of <br> Repetition | Question (a) |  | Question (b) |  | Question (c) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Equation | Work <br> Hours | Equation | Work <br> Hours | Equation | Work <br> Hours |
| 1st | - | 100 | $($ Worker 1) | 100 | - | 100 |
| 2nd | $100^{*} 2^{-0.152}$ | 90 | $100 * 2^{-0.152}$ | 90 | $100^{*} 2^{-0.152}$ | 90 |
| 3rd | $100 * 3^{-0.152}$ | 84.6 | $100 * 3^{-0.152}$ | 84.6 | $100^{*} 3^{-0.152}$ | 84.6 |
|  |  | $\varnothing$ |  | $\varnothing$ |  | 30 |
| 4th | $100^{*} 4^{-0.152}$ | 81 | $\left(\right.$ Worker 2) $^{*}$ | 100 | $100^{*} 2^{-0.152}$ | 90 |
| 5th | $100^{*} 5^{-0.152}$ | 78.3 | $100^{*-0.152}$ | 90 | $100^{*} 3^{-0.152}$ | 84.6 |
| 6th | $100^{*} 6^{-0.152}$ | 76.2 | $100^{*} 3^{-0.152}$ | 84.6 | $100^{*} 4^{-0.152}$ | 81 |
| Total |  | 510.1 |  | 549.2 |  | 560.2 |

(d) Lost Hours due to Loss of Productivity $=560.2-510.1-30=\underline{\mathbf{2 0}} \mathbf{. 1}$ work-hours

## Learning Curve Effect Concept [5 points]

Why is the concept of 'Learning Curve Effect' important to Contractors?
Either one of these will get full credit:

- For better planning and scheduling
- For proper resource leveling
- For measuring Impacts of Changes (Disruptions) to (1) re-plan the work when there is disruption and (2) to measure the loss of productivity (impact of changes) and get compensation for that from owner.


## [Project Control]

## Earned Value Analysis [35 points]

Using the data below, evaluate his project's earned value status as of the beginning of day 16 and the beginning of day 25 . All dates represent the beginning of the day.
(a) Depict the project status graphically. How is this project trending? Do you think the project will finish on budget? Discuss your analysis. All dates represent the beginning of the day. [30 points]
(b) Calculate FAC (EAC) using the data from the day 16. There are two different methods for FAC calculation. Apply both of them and compare the results. [5 points]

| Activity | Planned Dates |  | Total Cost | Budgeted <br> Unit Cost |
| :---: | :---: | :---: | :---: | :---: |
|  | Start | Finish |  | $\$ 18,000$ |
| $\$ 2,000 /$ day |  |  |  |
| A | 1 | 10 | $\$ 15,000$ | $\$ 1,500 /$ day |
| B | 8 | 18 | $\$ 40,000$ | $\$ 2,500 /$ day |
| C | 12 | 28 | $\$ 28,000$ | $\$ 2,000 /$ day |
| D | 16 | 30 | $\$ 101,000$ |  |
| Total | 1 | 30 |  |  |

As of Beginning of Day 16

| Activity | Actual or Forecasted* Dates |  | Actual Cost <br> Spend-to-Date | $\%$ Complete |
| :---: | :---: | :---: | :---: | :---: |
|  | Start | Finish | $\$ 20,000$ |  |
| A | 1 | 9 | $\$ 13,000$ | $90 \%$ |
| B | 7 | $17^{*}$ | $\$ 22,000$ | $50 \%$ |
| C | 11 | $23^{*}$ | $\$ 0$ | $0 \%$ |
| D | 16 | $28^{*}$ | $\$ 55,000$ |  |
| Total | 1 | $28^{*}$ |  |  |

As of Beginning of Day 25

| Activity | Actual or Forecasted* Dates |  | Actual Cost <br> Spend-to-Date | \% Complete |
| :---: | :---: | :---: | :---: | :---: |
|  | Start | Finish | $\$ 20,000$ |  |
| A | 1 | 9 | $\$ 15,000$ | $100 \%$ |
| B | 7 | 18 | $\$ 35,000$ | $80 \%$ |
| C | 11 | $29^{*}$ | $\$ 18,000$ | $60 \%$ |
| Dotal | 16 | $31^{*}$ | $\$ 88,000$ |  |

## Answers:

Part (a)

$$
S V=B C W P-B C W S \quad C V=B C W P-A C W P
$$

As of Beginning of Day 16

| Activity | BCWS | ACWP | BCWP | SV | CV |
| :---: | :---: | :---: | :---: | :---: | :---: |
| A | $\$ 18,000$ | $\$ 20,000$ | $\$ 18,000$ | $\$ 0$ | $-\$ 2,000$ |
| B | $\$ 12,000$ | $\$ 13,000$ | $\$ 13,500$ | $+\$ 1,500$ | $+\$ 500$ |
| C | $\$ 10,000$ | $\$ 22,000$ | $\$ 20,000$ | $+\$ 10,000$ | $-\$ 2,000$ |
| D | $\$ 0$ | $\$ 0$ | $\$ 0$ | $\$ 0$ | $\$ 0$ |
| Total | $\$ 40,000$ | $\$ 55,000$ | $\$ 51,500$ | $+11,500$ | $-\$ 3,500$ |

SI $=$ BCWP $/$ BCWS $=\$ 51,500 / \$ 40,000=1.29 \rightarrow$ Ahead of Schedule
$\mathrm{Cl}=$ BCWP $/$ ACWP $=\$ 51,500 / \$ 55,000=0.94 \rightarrow$ Over Budget

## As of Beginning of Day 25

| Activity | BCWS | ACWP | BCWP | SV | CV |
| :---: | :---: | :---: | :---: | :---: | :---: |
| A | $\$ 18,000$ | $\$ 20,000$ | $\$ 18,000$ | $\$ 0$ | $-\$ 2,000$ |
| B | $\$ 15,000$ | $\$ 15,000$ | $\$ 15,000$ | $\$ 0$ | $\$ 0$ |
| C | $\$ 32,500$ | $\$ 35,000$ | $\$ 32,000$ | $-\$ 500$ | $-\$ 3,000$ |
| D | $\$ 18,000$ | $\$ 18,000$ | $\$ 16,800$ | $-\$ 1,200$ | $-\$ 1,200$ |
| Total | $\$ 83,500$ | $\$ 88,000$ | $\$ 81,800$ | $-\$ 1,700$ | $-\$ 6,200$ |

SI = BCWP $/$ BCWS $=\$ 81,800 / \$ 83,500=0.98 \rightarrow$ Slightly Behind Schedule (Almost on Time)
$\mathrm{CI}=$ BCWP $/$ ACWP $=\$ 81,800 / \$ 88,000=0.93 \rightarrow$ Over Budget

## Discussion:

The project goes from being over-budget but ahead of schedule to being still over-budget and slightly behind schedule. In overall, the project status got worse. There was no big change in the cost status. Unless special measures or managerial actions are taken, the project will be completed over budget.


## $\mathrm{Cl}=1.0$

*Another type of graph can be used, which was introduced both in class and the review session.

## Part (b)

BAC $($ Budget at Completion $)=$ Original Budget for the Project $=\$ 101,000$
Method \#1: FAC $=$ ACWP $+(B A C-B C W P)=55,000+(101,000-51,500)=\$ \mathbf{1 0 4 , 5 0 0}$
Method \#2: FAC $=A C W P+(B A C-B C W P) / C I=55,000+49,500 / 0.94=\underline{\$ 107,660}$
Reflecting the relative deviation of cost of work completed, method \#2 shows the result of higher total cost prediction. In other words, when using method \#2, we assume that the past cost performance (deviations) is a good predictor of the cost deviations in the remaining work.

## [Changes and Disputes]

Pricing of Changes [10 points]
(a) What is forward pricing?
(b) What is force account?

[^0]
## According to Bartholomew;

(a) If the contractor and owner agree on the price and time requirement for the changed or additional work before starting performance of the change, the change is said to be forward priced. Under fixed-price contracts, the contractor assumes the full financial risk of performance in the same manner as for the original contract when changes are forward priced.
(b) Force account is a particular form of retrospective pricing in which the contract spells out a specific procedure for arriving at the price adjustment when the contractor and the owner fail to agree on the price by forward pricing. When force account is used, daily records are kept of labor, material, and equipment usage expended on the changed work by the general contractor and all subcontractors involved. The records are agreed upon daily and signed by representatives of both owner and contractor.

## Types of Delay [15 points]

List the types of delay and describe the conditions that determine the types.

Answer:


- Owner Changes
- Design Problems
- Differing Site Conditions
- Unanticipated Weather
- Labor Strikes
- Acts of God


Owner delays and Contractor delays happening at the same time

Answer can be narrative.

## Constructive Changes [15 points]

(a) What is a constructive change? When it occurs?
(b) What is a contractor supposed to do in this situation?
(c) What are the two elements that must be proved to establish a constructive change?

## According to Bartholomew;

(a) A constructive change is a change that is not acknowledged by the owner as such when it occurs, but which nonetheless is a change. In this situation, the owner takes the position that whatever the contractor is directed to do or is prevented from doing is not a change, but rather is required or prohibited by the original contract, as the case may be.
(b) In these situations, the contractor is required to proceed according to the owner's instructions but is free to assert and later attempt to prove that the owner's instructions constituted a change order. If the contractor is correct, court will deem that a constructive change has occurred, and the contractor will be awarded the costs incurred plus a reasonable profit thereon.
(c) First the change element must be proved. The court must be convinced that a true change occurred in the work or requirements of the contract. Second, the order element must be proved. This is established entirely by the owner's acts or words, either written or oral. There must have been an actual order or directive to the contractor or a course of conduct by the owner that had the practical effect of such an order or directive.

## [Insurance and Bonds]

## Bid Bond and Performance Bond [10 points]

(a) What is bid bond? Who provides it and why?
(b) What is performance bond? Who buys it? And whom does it protect from what?

## According to Bartholomew;

(a) Owners want the assurance that the bidding contractor who is awarded the contract will accept and sign it and will furnish all insurance policies and additional surety bonds required by the bid documents. If the successful bidder refuses to sign the contract, the owner must accept a higher price or re-bid the project. Neither alternative is desirable. The bid bond protects the interests of the owner against this potential loss. Contractors must provide the bid bond when they bid for the project.
(b) Owners naturally want assurance that, once they have awarded a contract, the contractor will perform according to the contract's terms. Therefore, owners require contractors buy the bond to protect themselves.


[^0]:    * For all descriptive answers, you will get the full credits if you describe the main ideas and issues correctly. That is, the answers don't need to be exactly same as the answers provided here.

